

A Probabilistic Model of the Categorical Association between Colors

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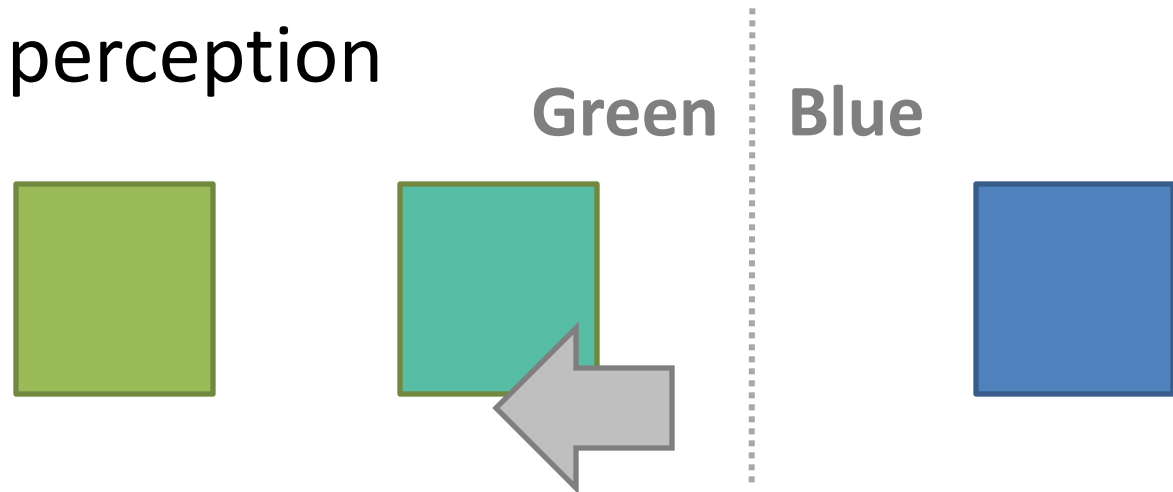
Color Imaging Conference
November 12, 2008

Overview

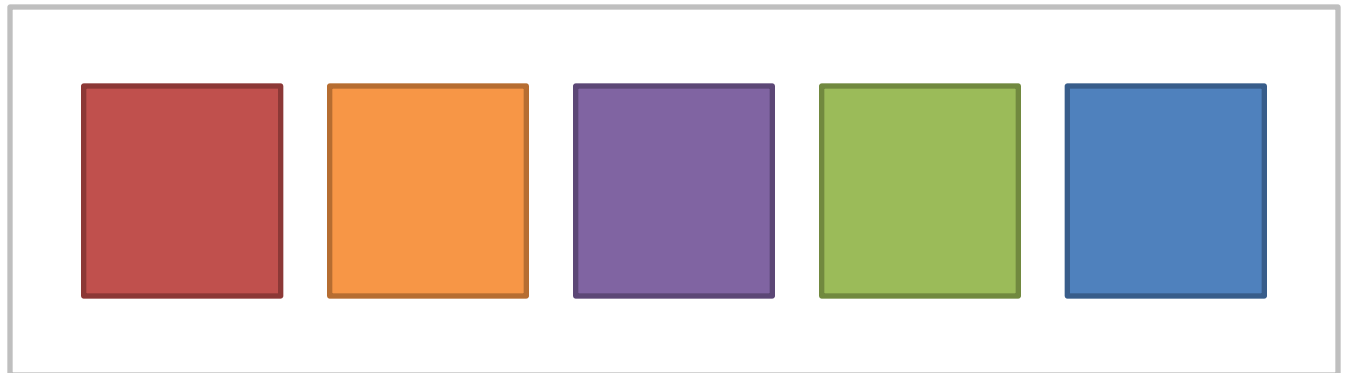
- **Introduction**
 - **Color names**
 - **Previous work**
 - **Goals**
- **Categorical association**
 - Probabilistic framework
 - Results
- **Summary**

Why Color Names?

- Affect our perception

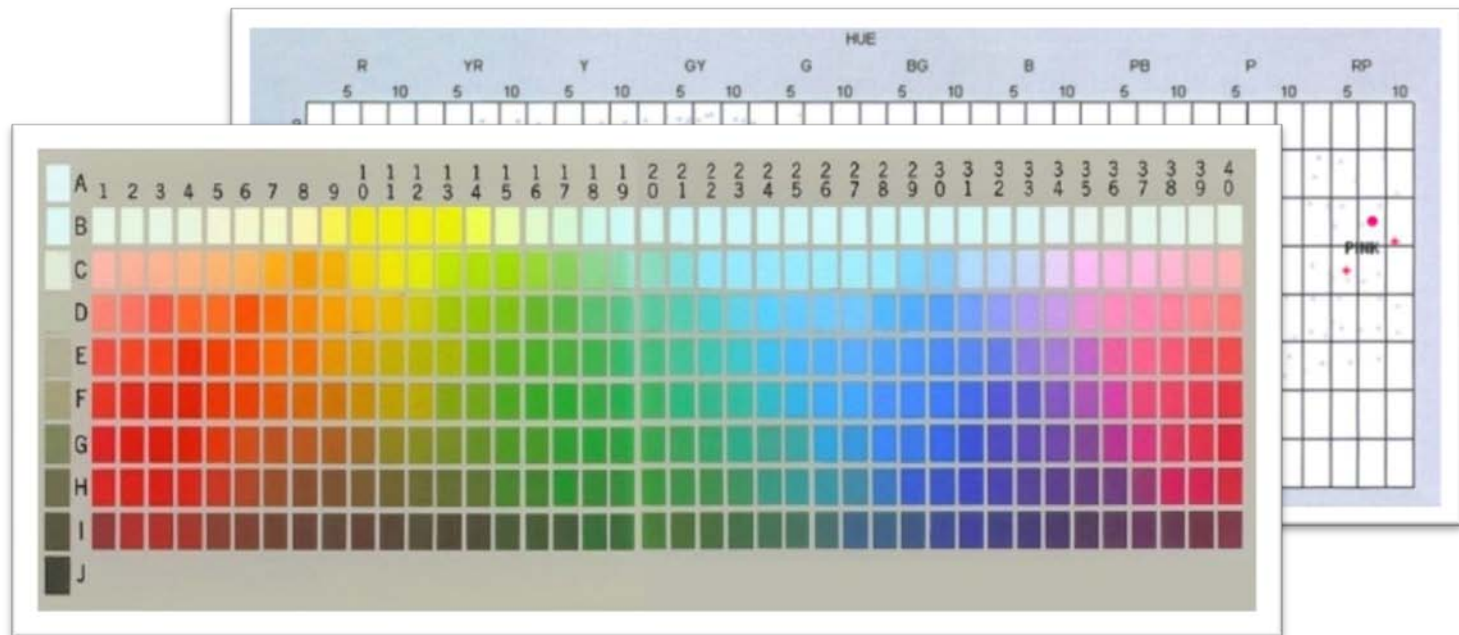


- Improve communication



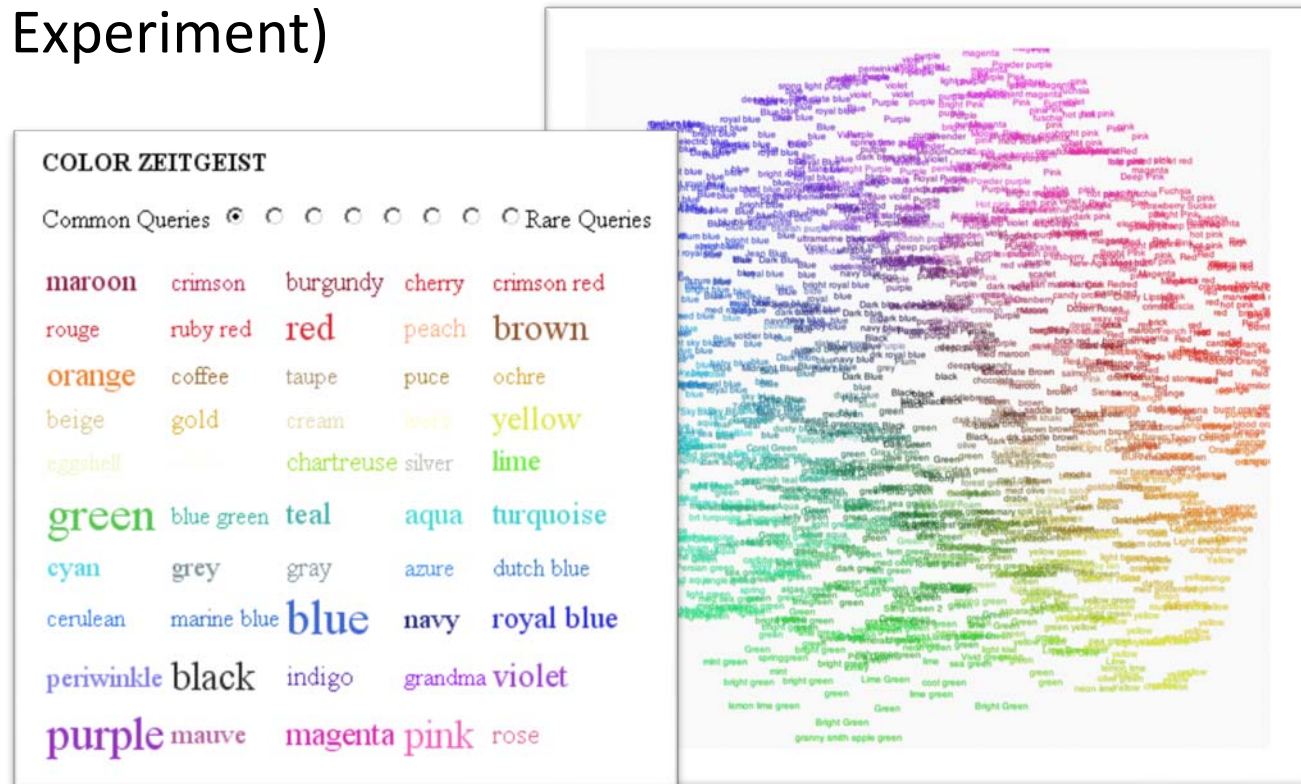
Naming Studies

- Earlier studies
 - For 19 languages, only 1 speaker (Berlin & Kay)
 - 10 speakers for English (Benavente)
 - 25-30 speakers for 110 languages (World Color Survey)

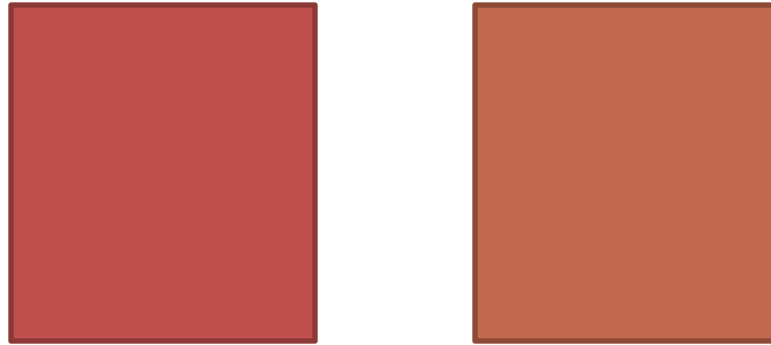


More Naming Data

- Online surveys
 - 238 speakers in English (Dolores Labs)
 - 4000 speakers in 20 languages (HP Naming Experiment)



Color Name Models

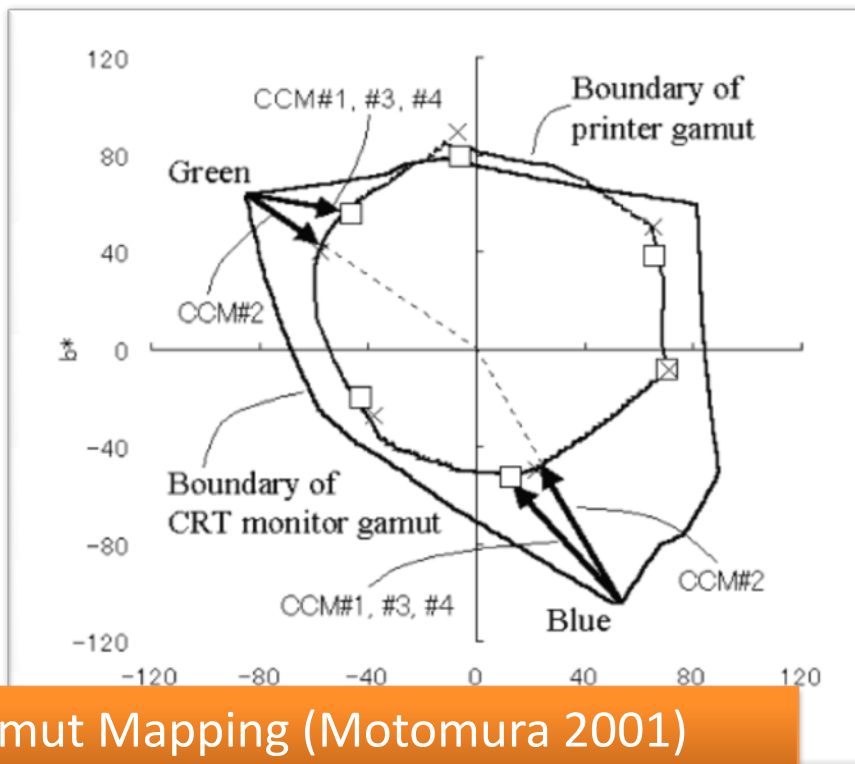


“Do two colors have the same name?”

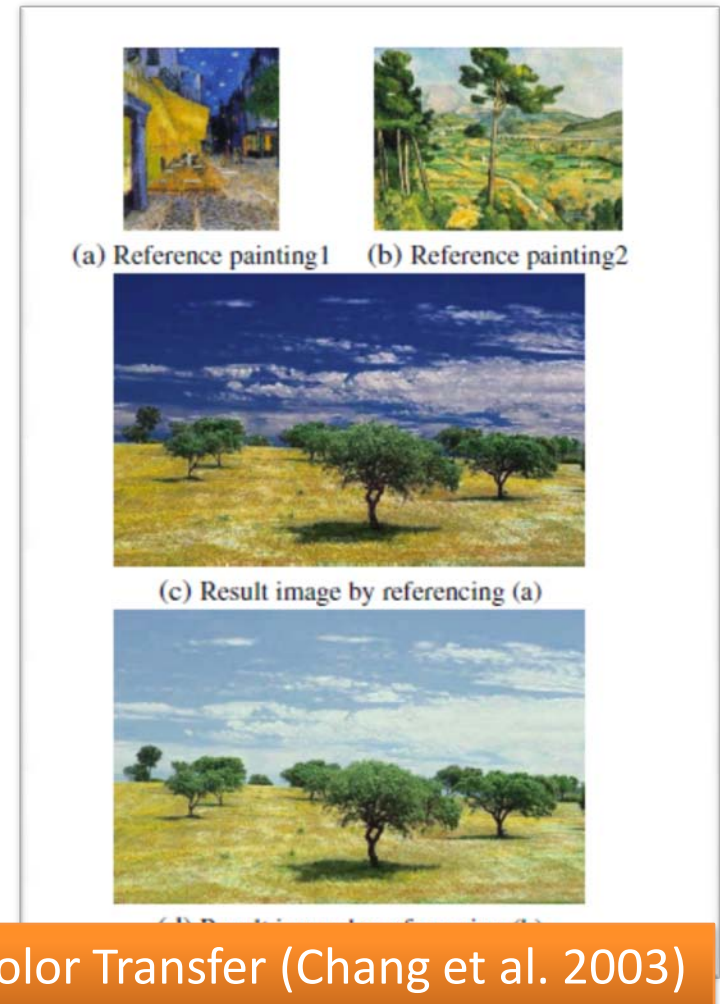
“Which color has a more consistent name?”

Color Name Models

- Preserving color names

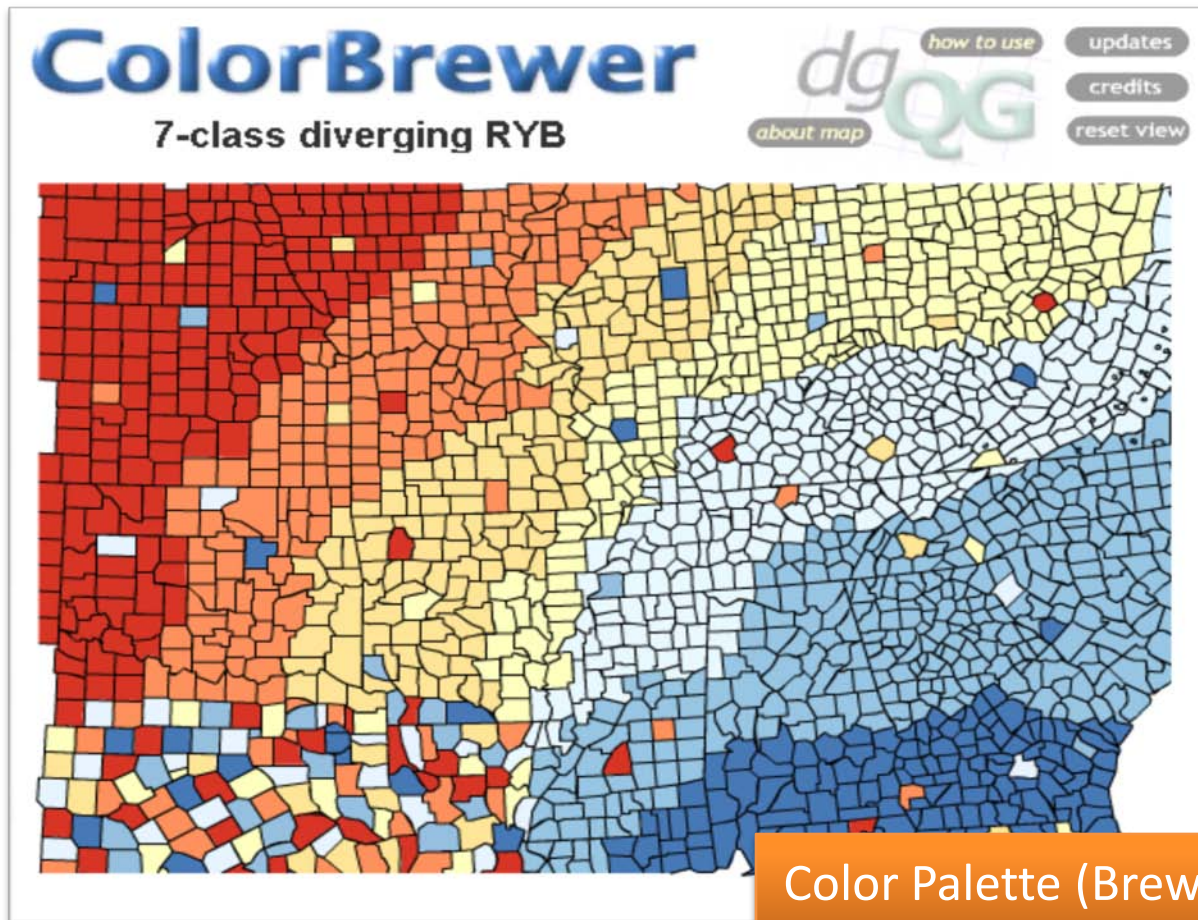


Gamut Mapping (Motomura 2001)

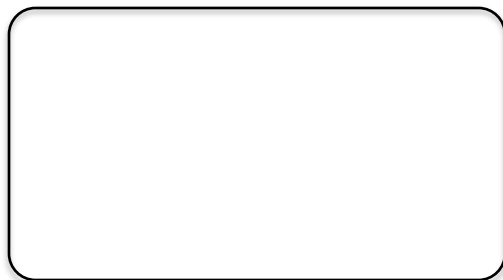
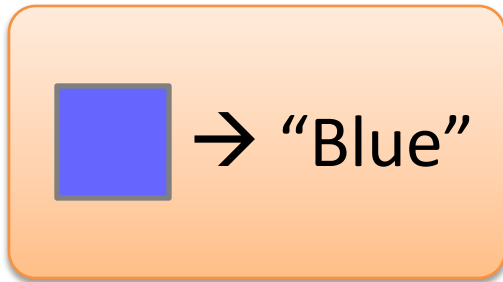


Color Name Models

- Colors with consistent names

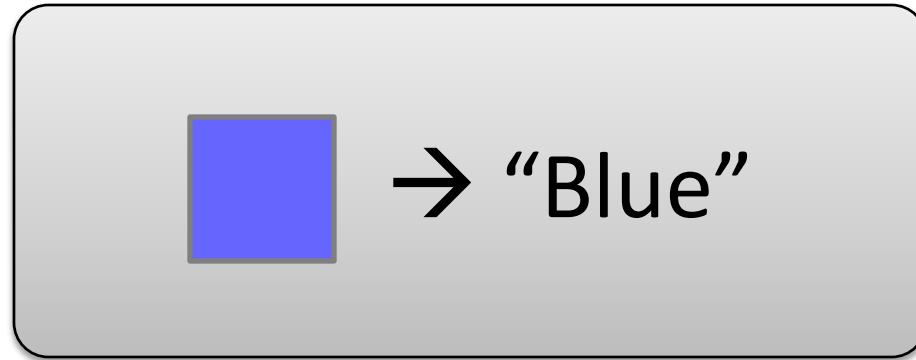


Previous Work

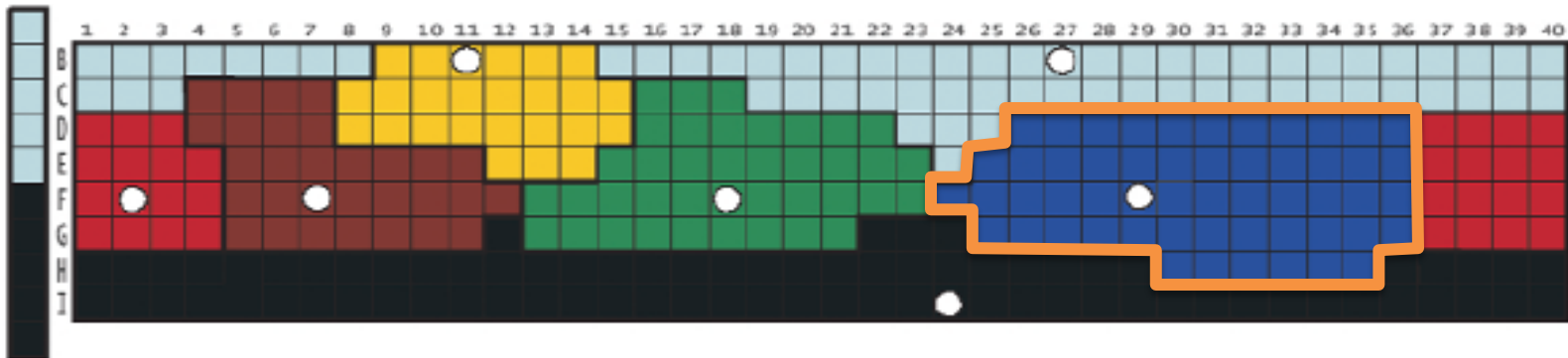


- **Single term**
 - Focus plus boundary
 - Simple partitioning
- Prototypes
 - Focus plus distribution
 - Linear combination of names
- Non-parametric models
 - Statistical representation
 - Requires sufficient data

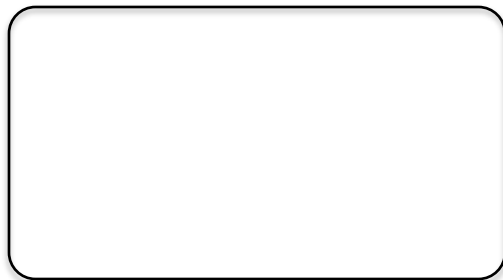
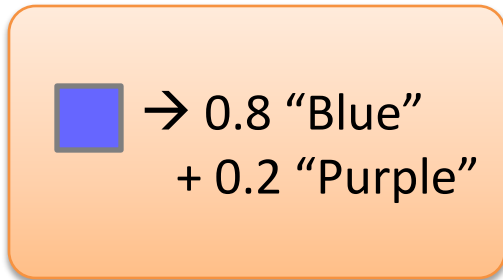
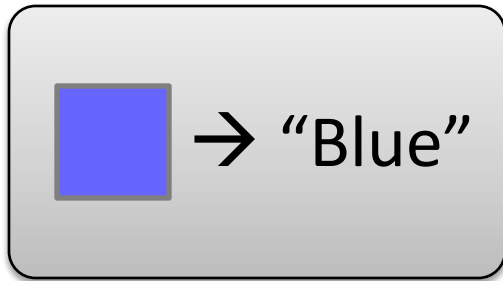
Single Terms



- Partition the color space into name regions
 - Illustrating basic color terms (Berlin & Kay 1969)
 - Lin et al. 2000, Chang et al. 2004, Kelly & Judd, ...

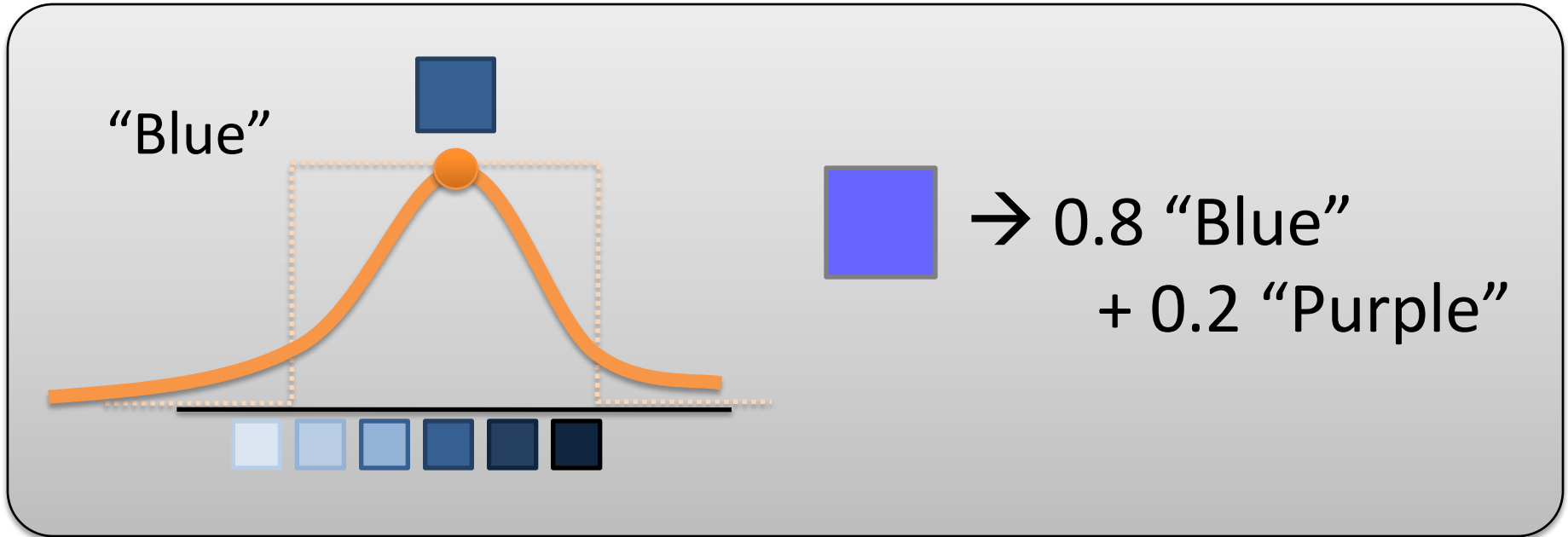


Previous Work



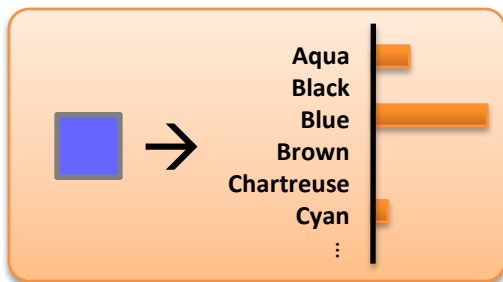
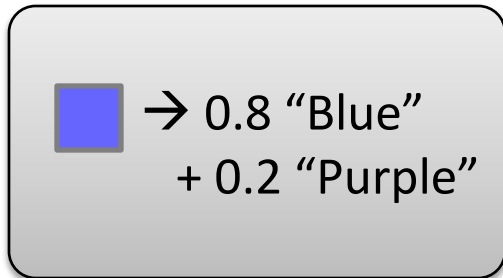
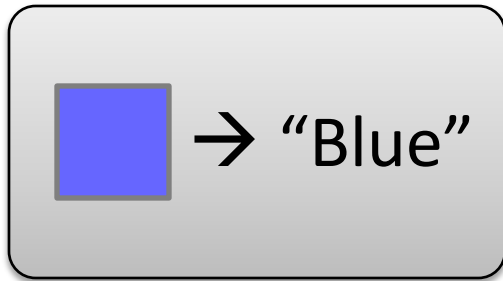
- Single term
 - Focus plus boundary
 - Simple partitioning
- **Prototypes**
 - **Focus plus distribution**
 - **Linear combination of names**
- Non-parametric models
 - Statistical representation
 - Requires sufficient data

Prototypes



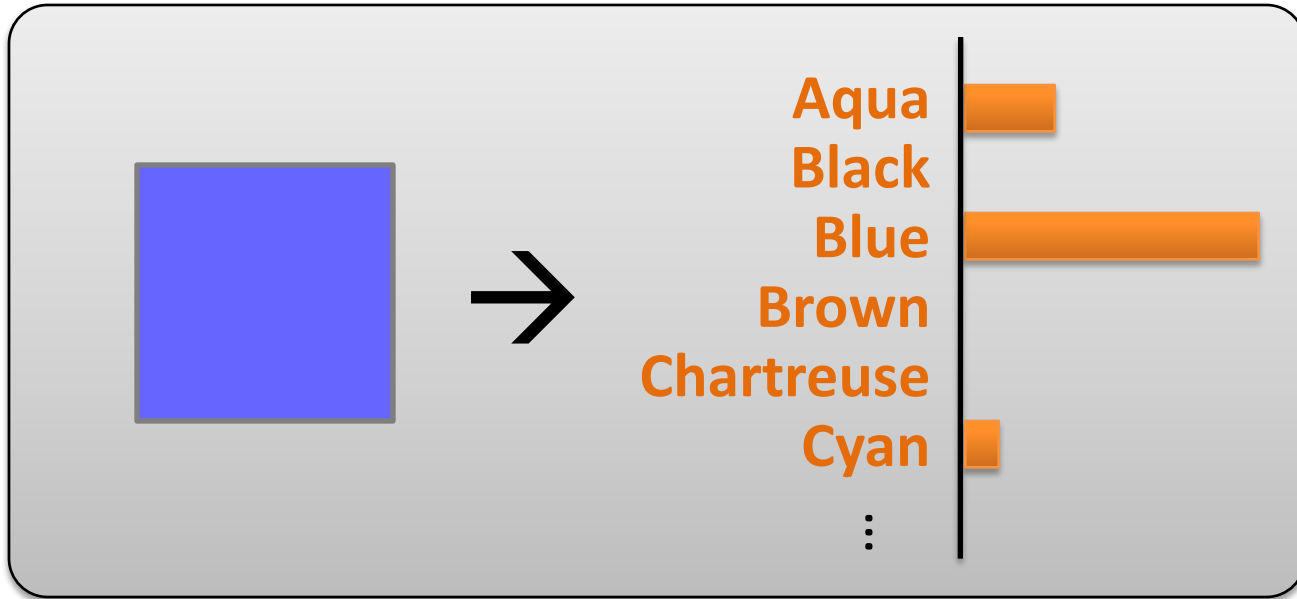
- Focus plus parameterized distribution
- Linear combination of a list of names
 - Gaussians (Motomura 2001)
 - Sigmoid-Gaussians (Benavente et al. 2002)

Previous Work



- Single term
 - Focus plus boundary
 - Simple partitioning
- Prototypes
 - Centroid plus distribution
 - Linear combination of names
- **Non-parametric models**
 - **Statistical representation**
 - **Requires sufficient data**

Non-Parametric Models




- Don't assume particular distribution
- Represent each term by a histogram
 - Benavente et al. 2006
 - Moroney 2007

Issues


- Color name regions
 - Different shapes and sizes
 - Want to preserve detailed shapes of the region
- Color vocabulary
 - More than 11 basic color terms
 - Emerging terms, multilingual data
 - Want to determine important color words from data, instead of using a pre-determined list
 - Robust when rare words are included

Our Goals


- Non-parametric model
- Inclusion of all color words, possibly from multiple languages
- Support a rich set of computational tools









→ “Blue”

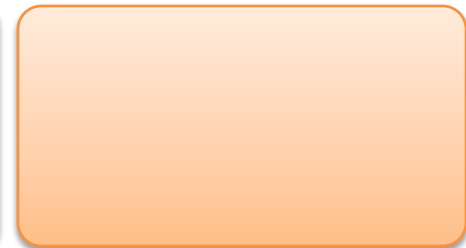


→ 0.8 “Blue”
+ 0.2 “Purple”



→

Aqua	
Black	
Blue	
Brown	
Chartreuse	
Cyan	
⋮	



Overview

- Introduction
 - Color naming and categories
 - Previous work
 - Goals
- **Categorical association**
 - **Probabilistic framework**
 - **Results**
- Summary

Categorical Association




- **Notations**
 - **Colors and Words**
- Probabilistic Framework
 - “Examples” of colors
 - Color saliency
- Results
 - World Color Survey
 - DoloresLabs Dataset
 - Comparison

Notation

- Color naming data consists of two variables
 - Colors $C = \{ \text{red}, \text{orange}, \text{purple}, \text{green}, \text{blue}, \text{black} \}$
 - Words $W = \{ \text{“aqua”}, \text{“black”}, \text{“blue”}, \text{“brown”}, \text{“chartreuse”}, \text{“cyan”}, \dots \}$

Relationships

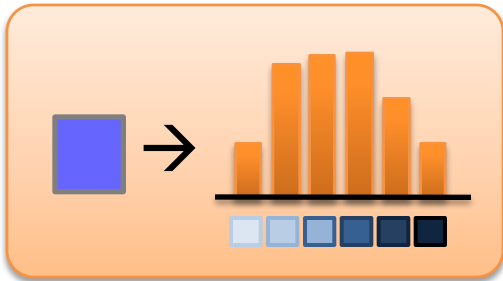
- Two types of relationships
 - Given a color , what are the likely words applied to the color?

$$P(W | C = \text{blue})$$

- Give a word “blue”, what are the likely colors the word refers to?

$$P(C | W = \text{“blue”})$$

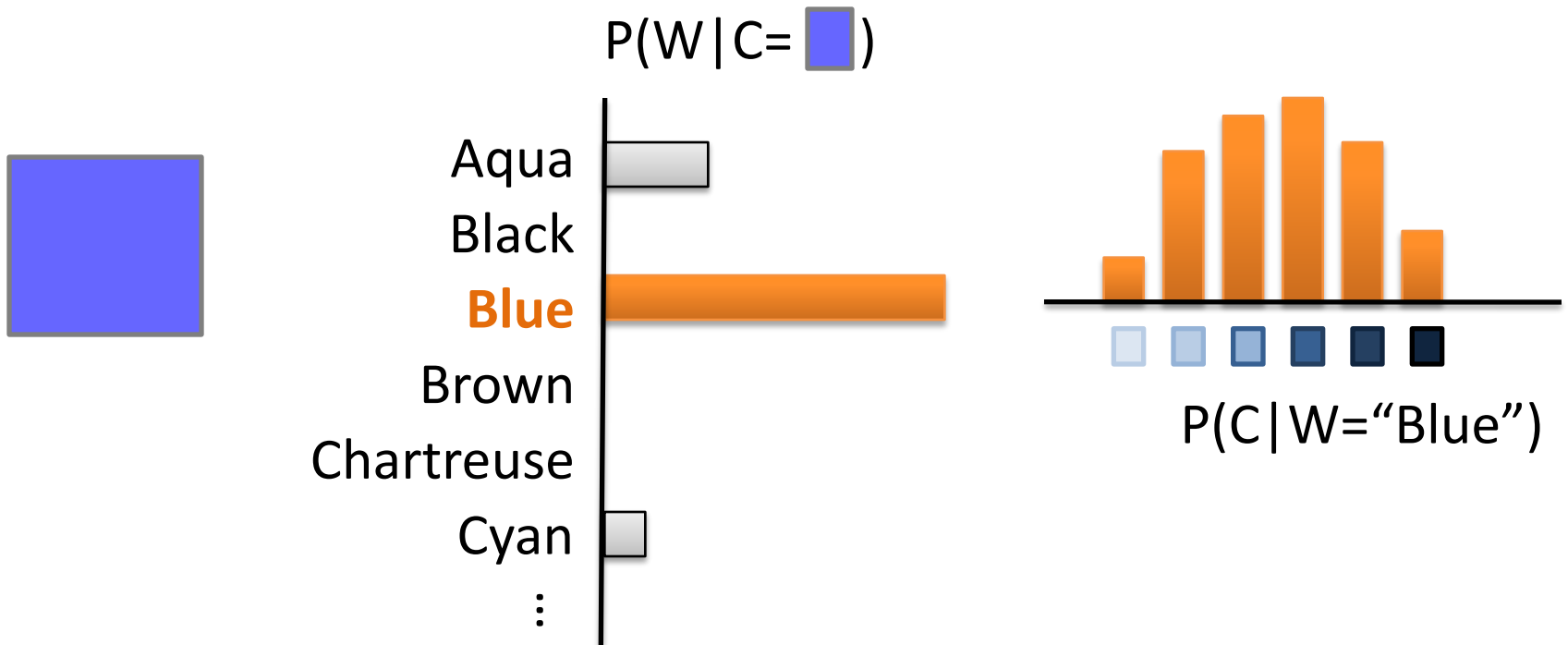
Categorical Association



- Notations
 - Colors and Words
- **Probabilistic Framework**
 - “Example” colors
 - **Color saliency**
- Results
 - World Color Survey
 - DoloresLabs Dataset
 - Comparison

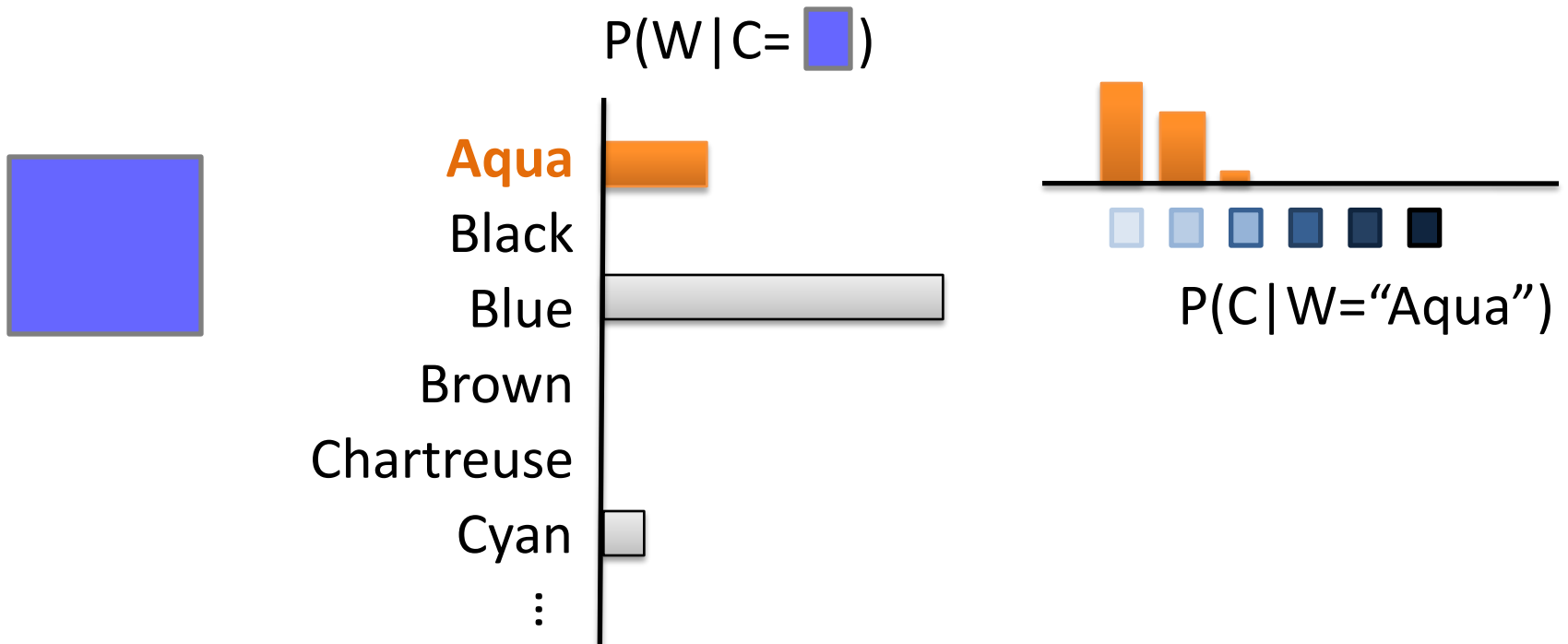
Categorical Association

- Represent a color by other “example” colors



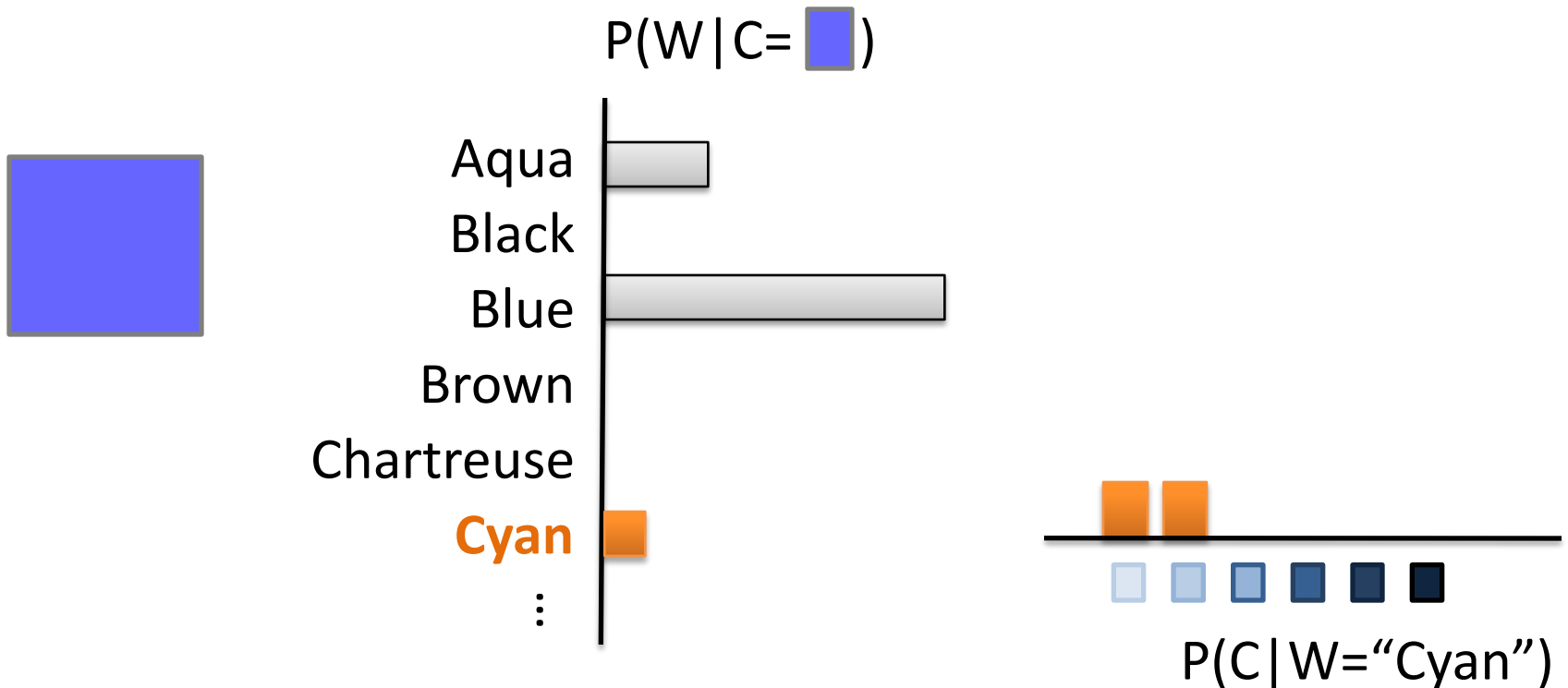
Categorical Association

- Represent a color by other “example” colors



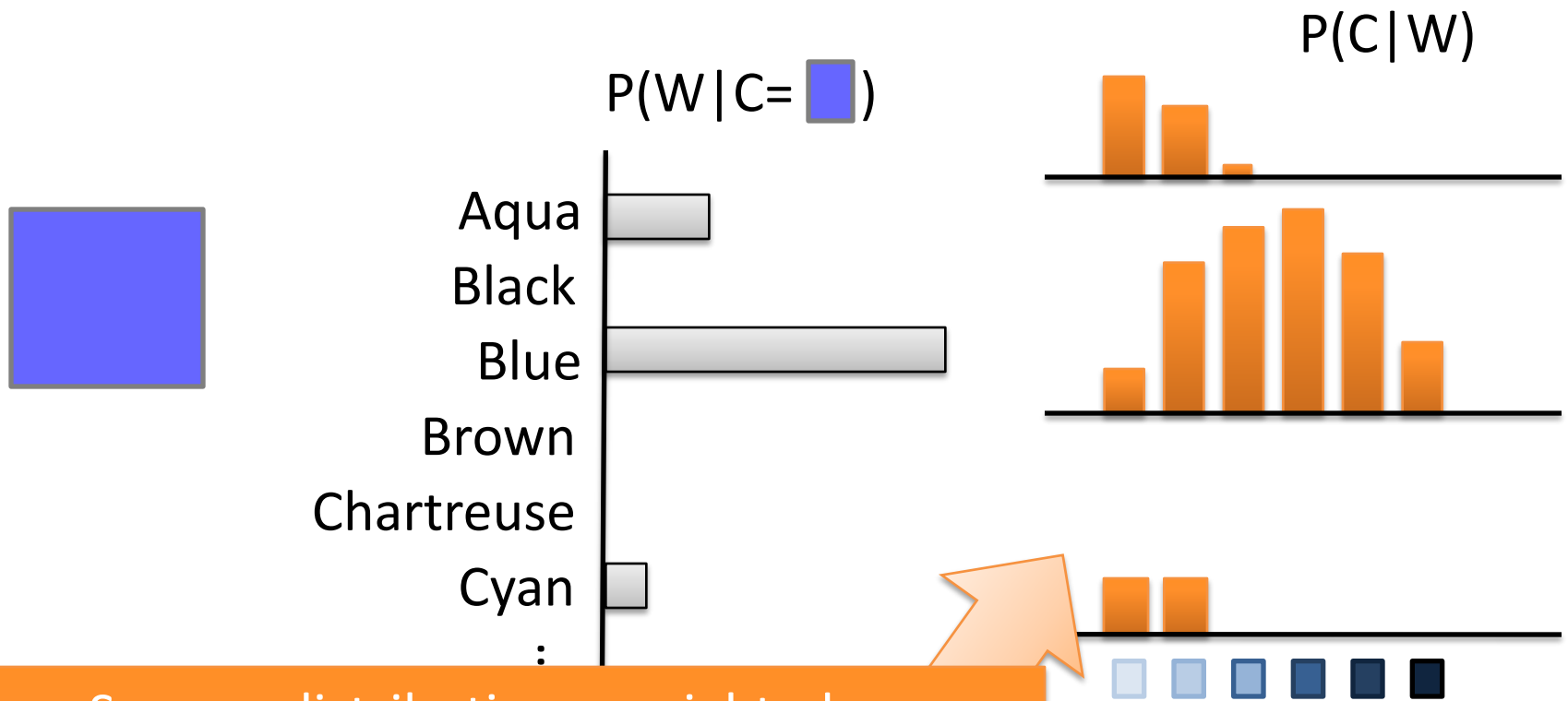
Categorical Association

- Represent a color by other “example” colors



Categorical Association

- Represent a color by other “example” colors



Sum up distributions, weighted by the frequency of the word.

Categorical Association

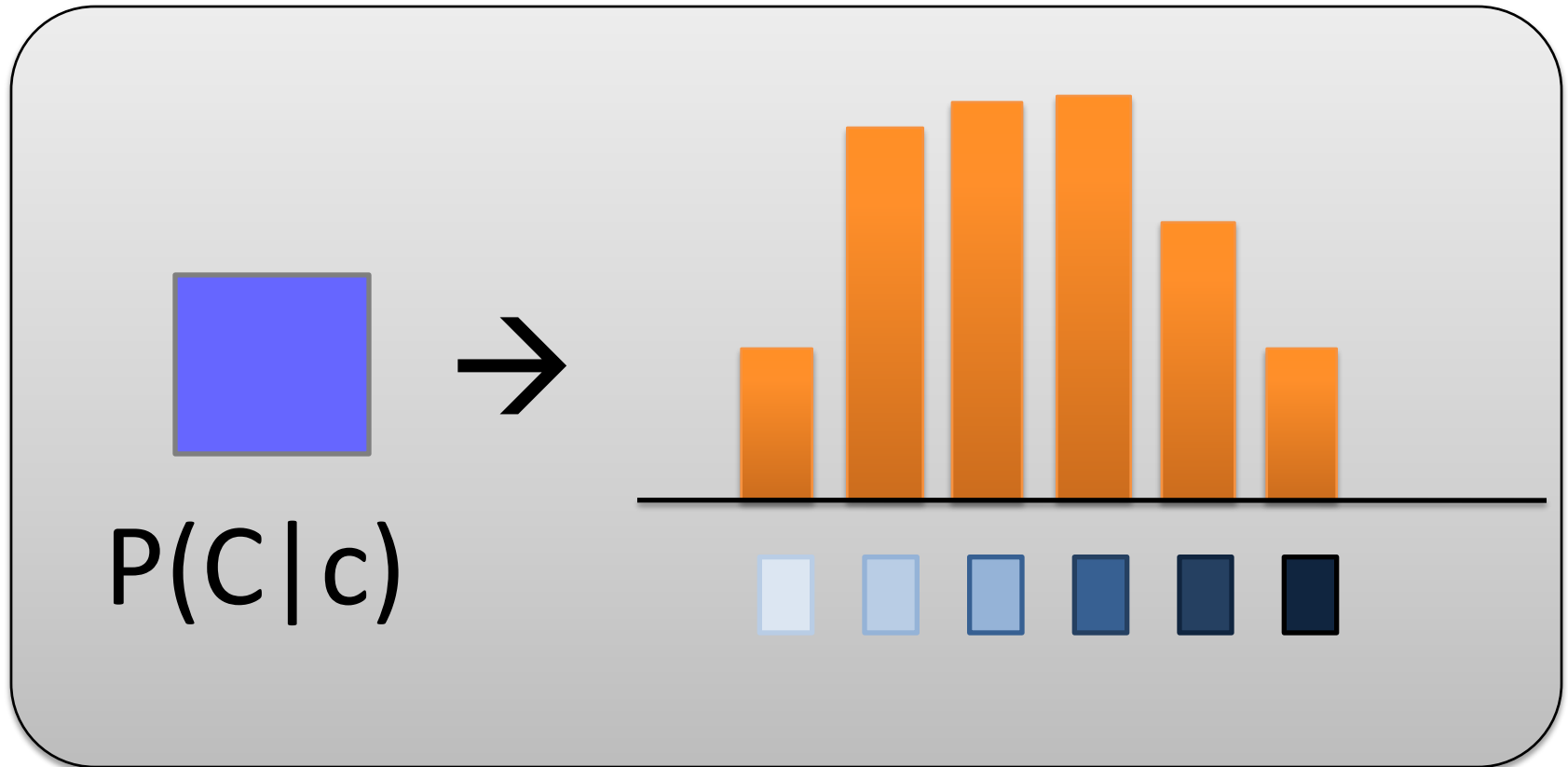
- Represent a color by other “example” colors

$$P(C | c = \text{blue}) = \sum_w P(C | w) P(w | c = \text{blue})$$

- Sum contribution from all color words, weighted by frequency of word

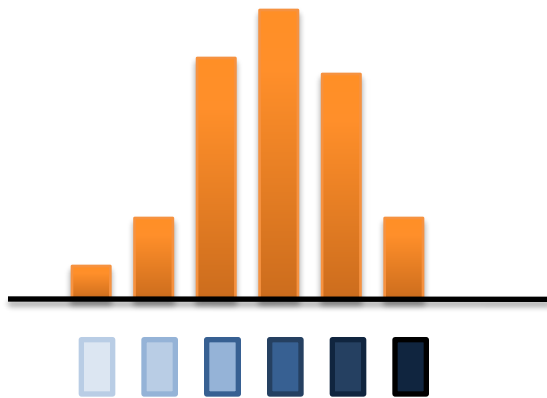
Categorical Association

- Represent a color by other “example” colors.



Color Saliency

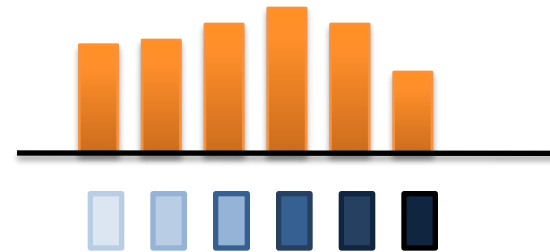
- Entropy = “Uncertainty”



Low Entropy

Strongly associated
with a few colors

High Saliency



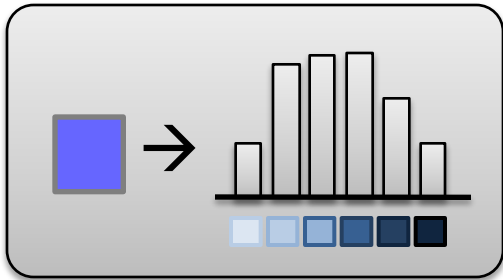
High Entropy

Weakly associated
with many colors

Low Saliency

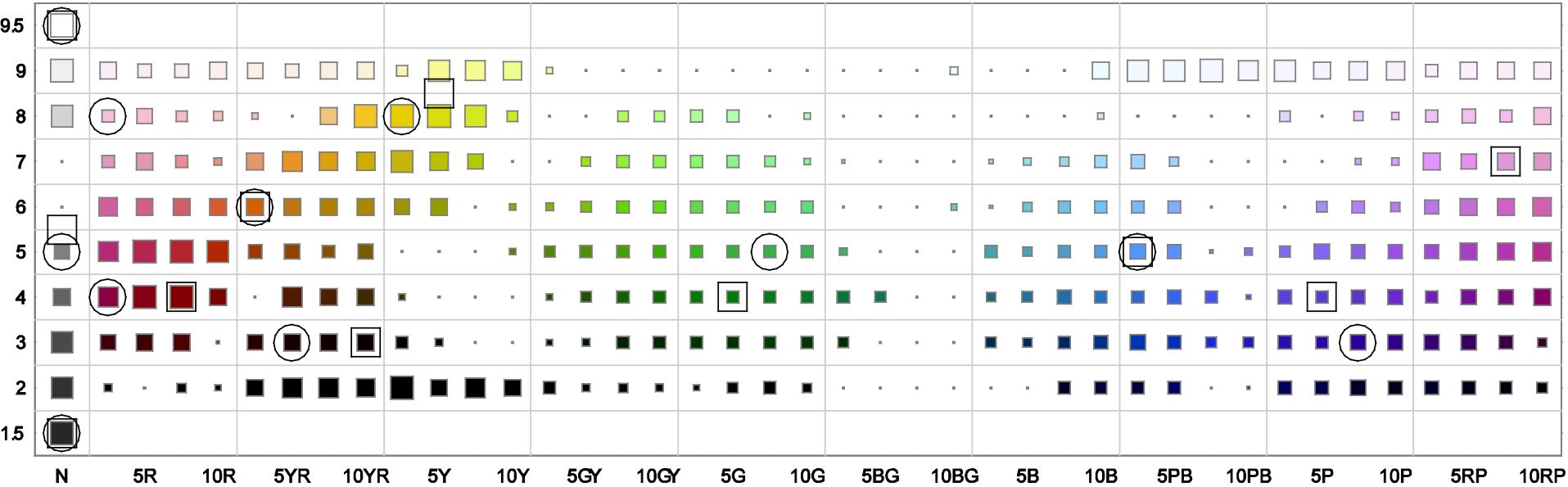
- Saliency = $-H(C|c = \text{blue}) = -P(C|c) \log(P(C|c))$

Categorical Association



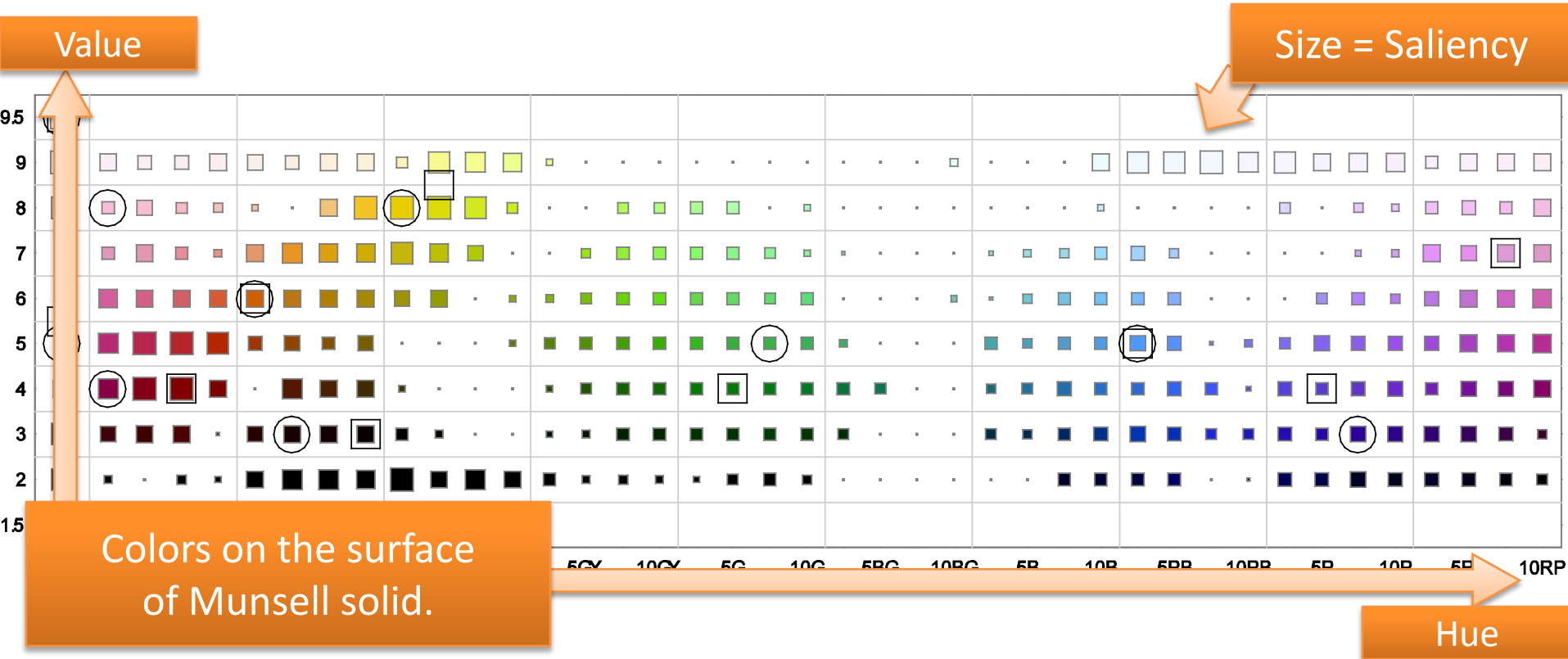
- Notations
 - Colors and Words
- Probabilistic Framework
 - “Example” colors
 - Color saliency
- **Results**
 - **World Color Survey**
 - **DoloresLabs Dataset**
 - **Comparison**

Color Saliency on Munsell Surface



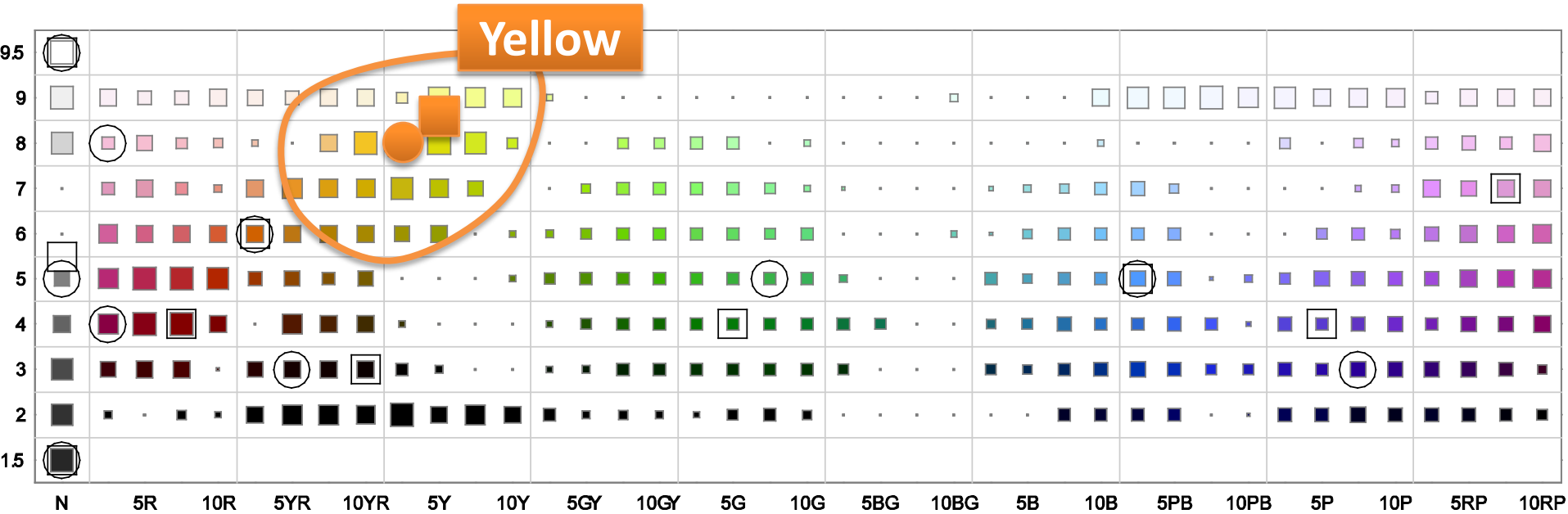
- Based on 6 languages from World Color Survey
- How does saliency match known color foci?

Color Saliency on Munsell Surface



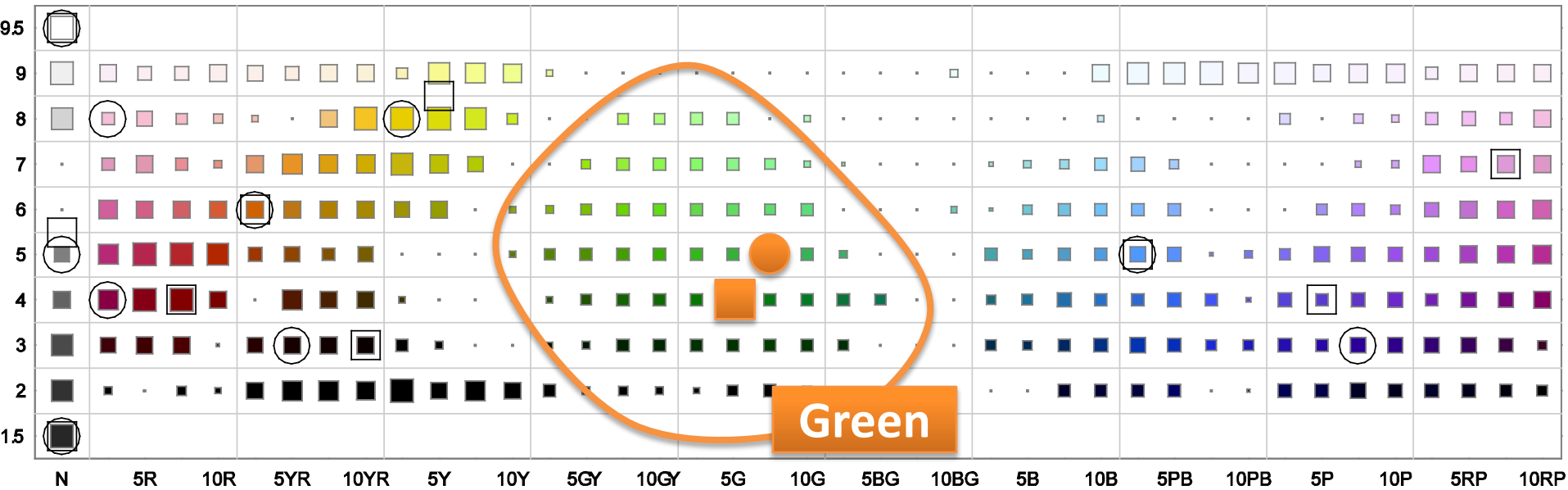
- Based on 6 languages from World Color Survey
- How does saliency match known color foci?

Correspondence with Known Foci



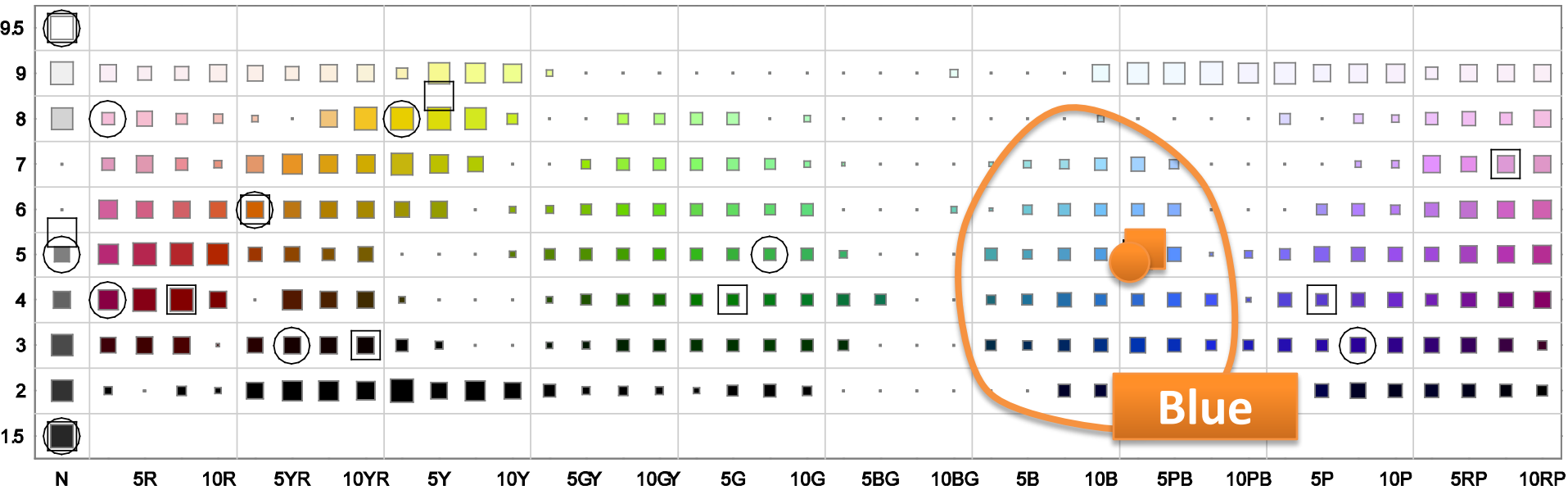
- English basic color foci observed by
 - ● = Berlin and Kay (1969)
 - ■ = Sturges and Whitfield (1995)

Correspondence with Known Foci



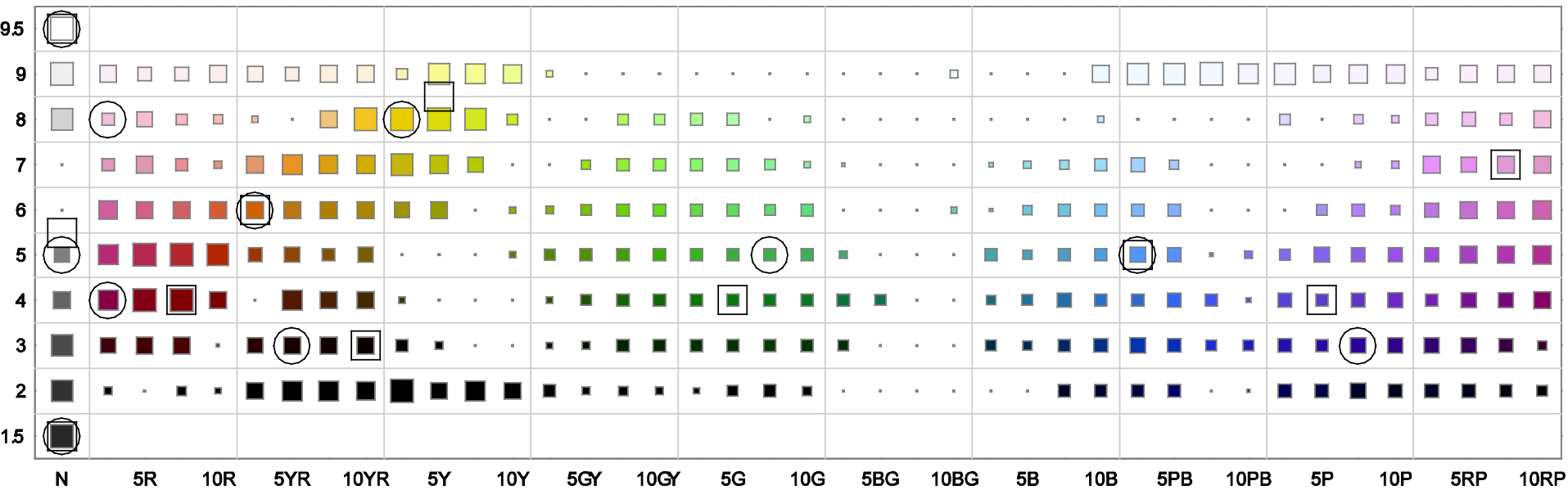
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Correspondence with Known Foci



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Color Saliency on Munsell Surface

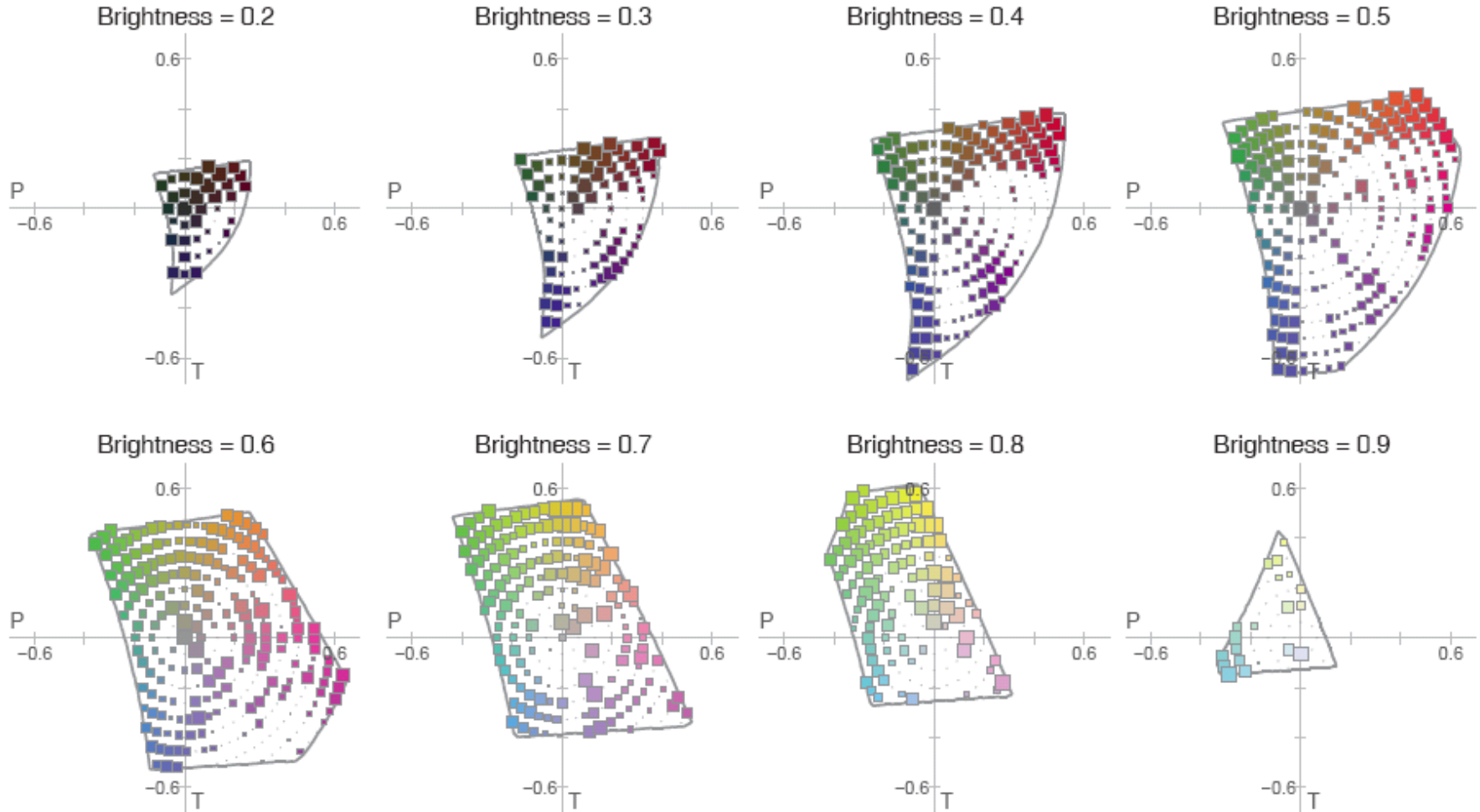


- English basic color foci observed by
 -  = Berlin and Kay (1969)
 -  = Sturges and Whitfield (1995)

DoloresLabs Naming Data

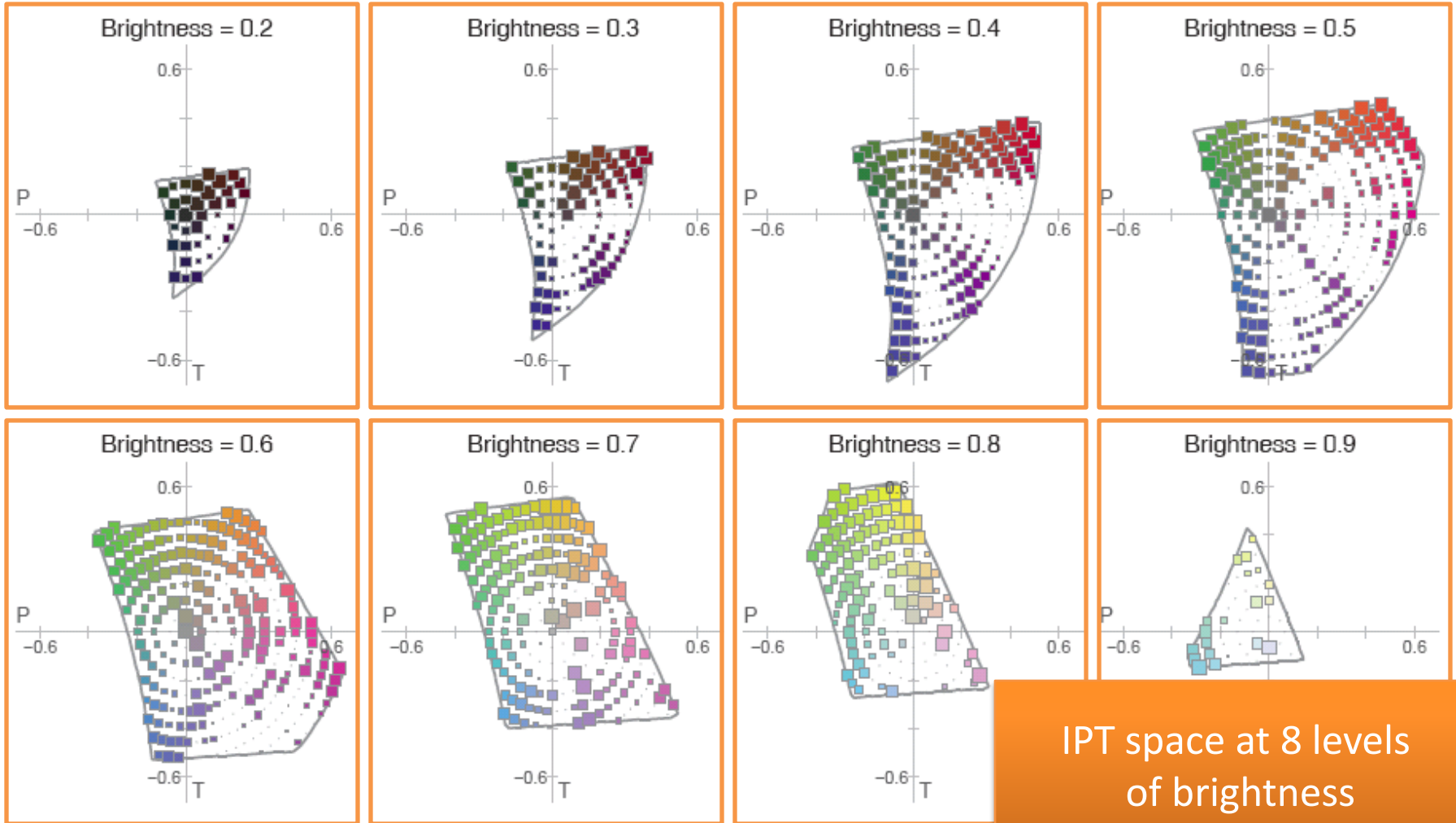
- Unconstrained online naming survey
 - 10,000 colors from 238 speakers
 - 1,966 distinct responses (raw ASCII strings)
 - 1,740 distinct phrases (spellings & punctuations)
 - 302 distinct words
- Non-uniformly sampled from RGB space

Color Saliency in sRGB Gamut



- Plotted in IPT space (assuming sRGB)

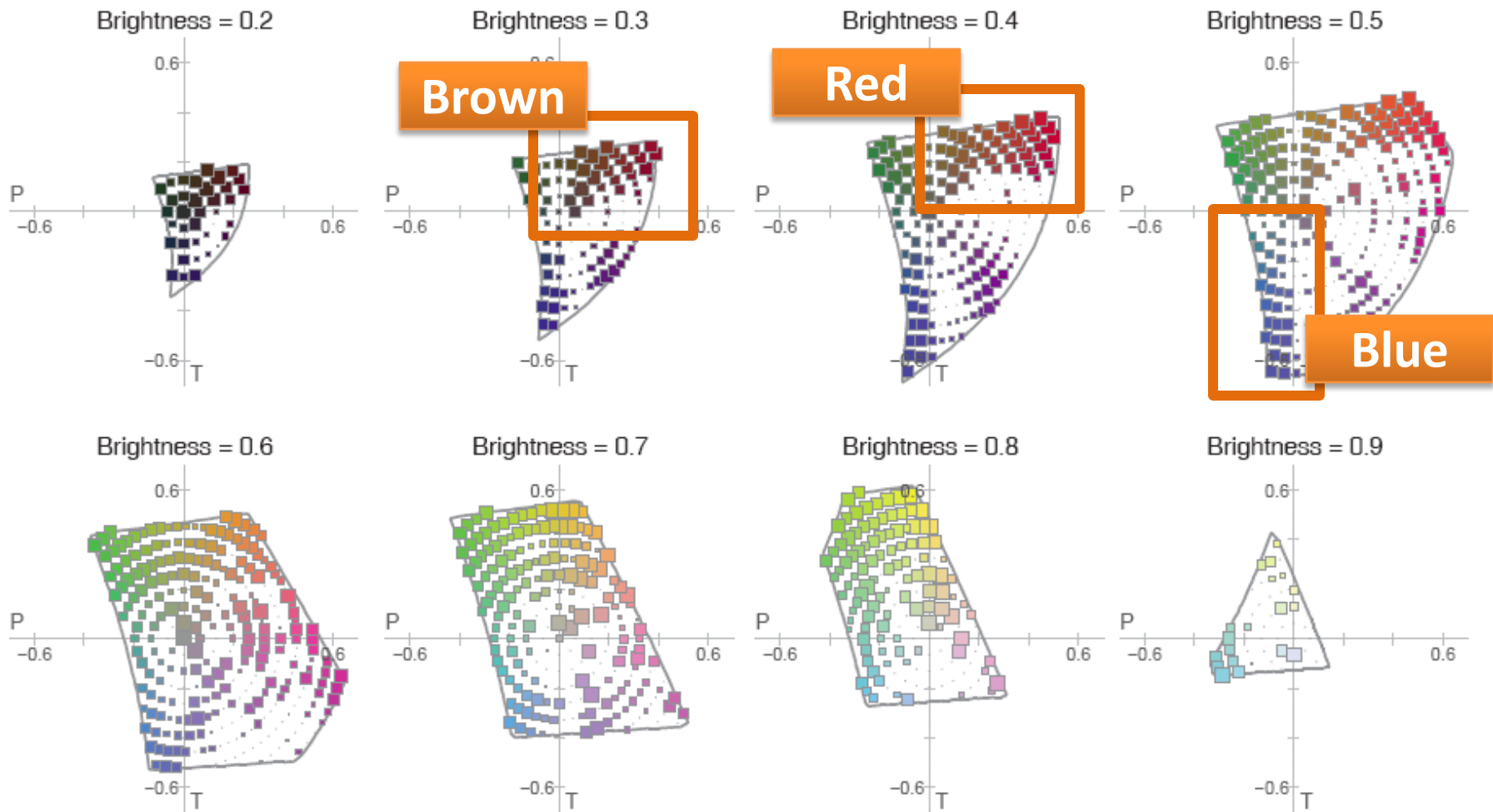
Color Saliency in sRGB Gamut



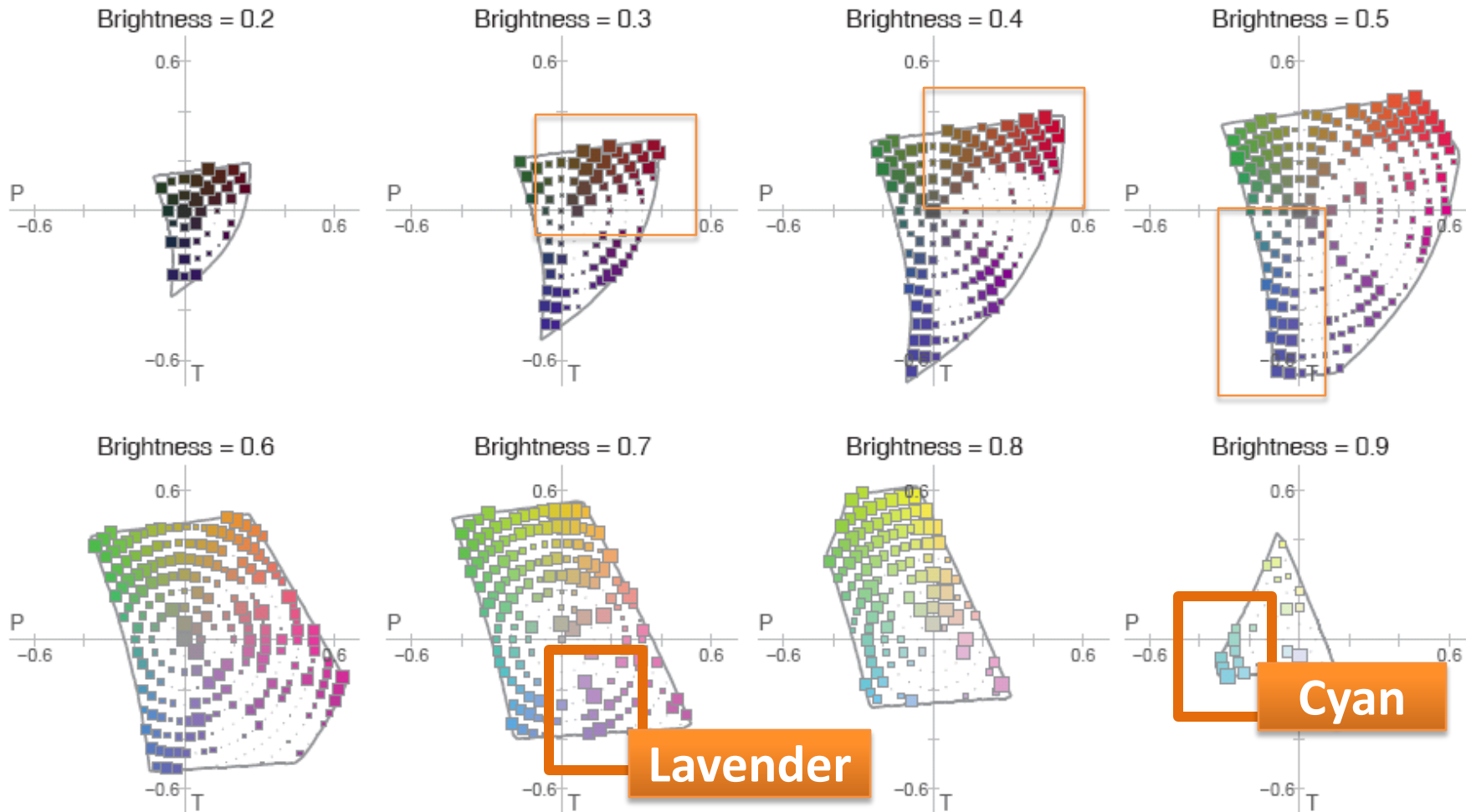
IPT space at 8 levels of brightness

- Plotted in IPT space (assuming sRGB)

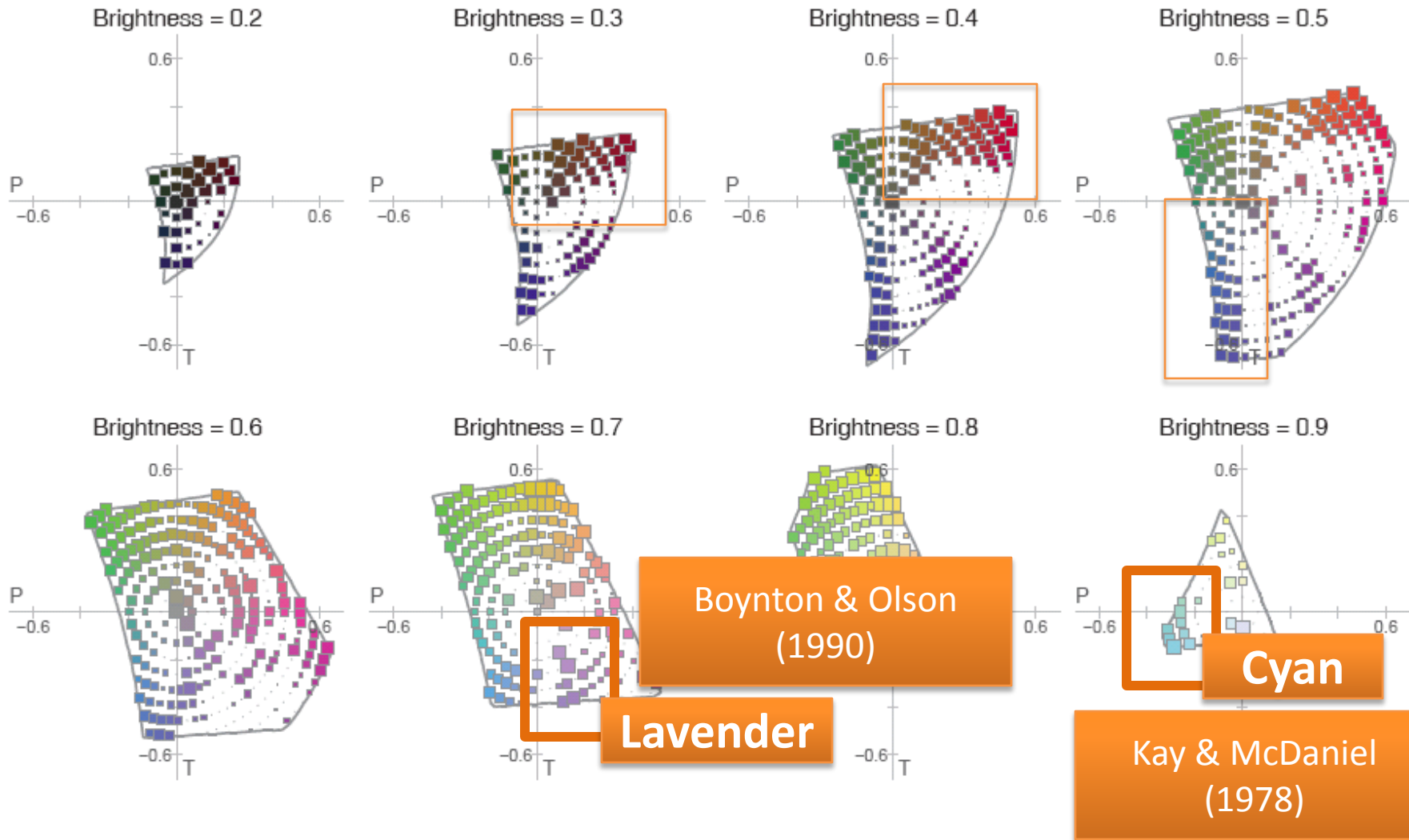
Clusters of Salient Basic Colors



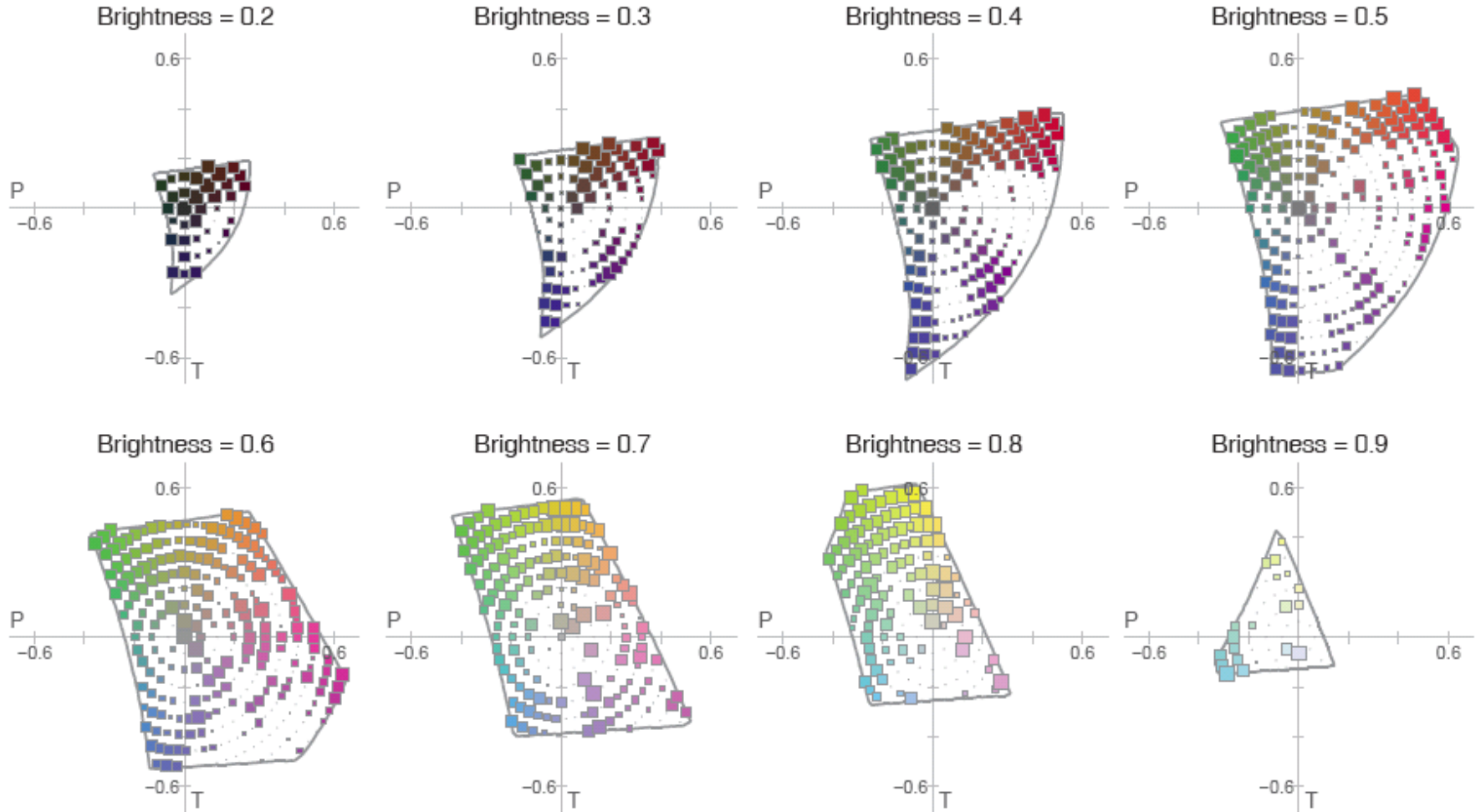
Clusters of Salient Non-Basic Colors



Clusters of Salient Non-Basic Colors

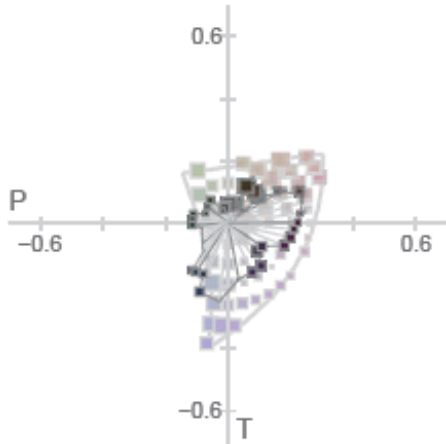


Color Saliency in sRGB Gamut

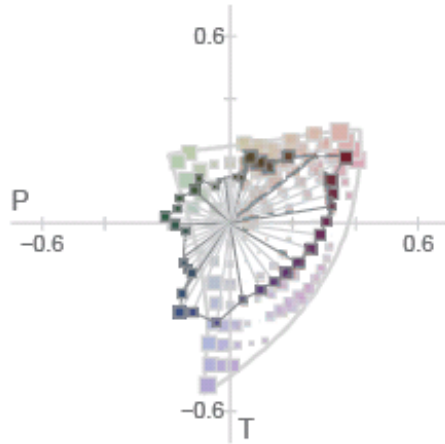


Comparison of Munsell/sRGB

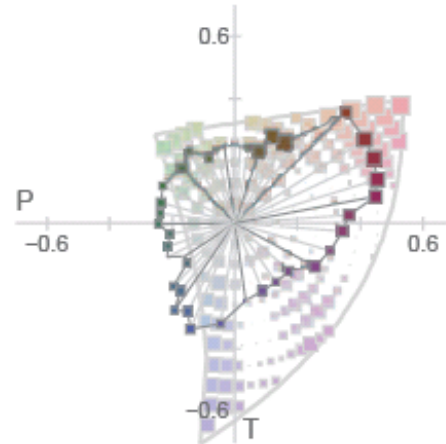
Munsell value = 2.0
IPT brightness = 0.2317



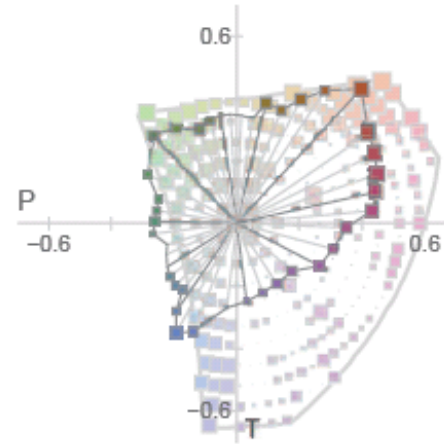
Munsell value = 3.0
IPT brightness = 0.3179



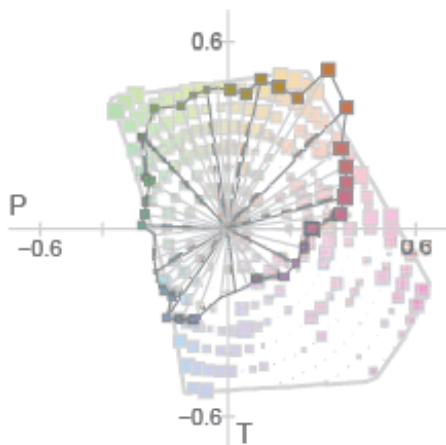
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IPT brightness = 0.4100



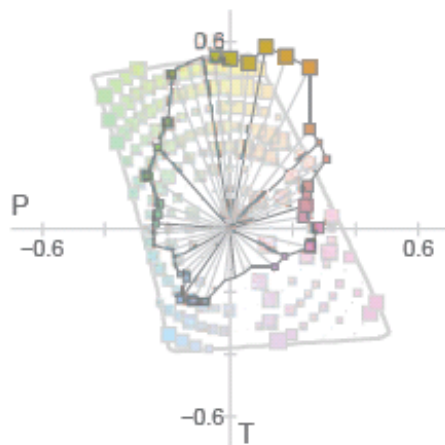
Munsell value = 5.0
IPT brightness = 0.5051



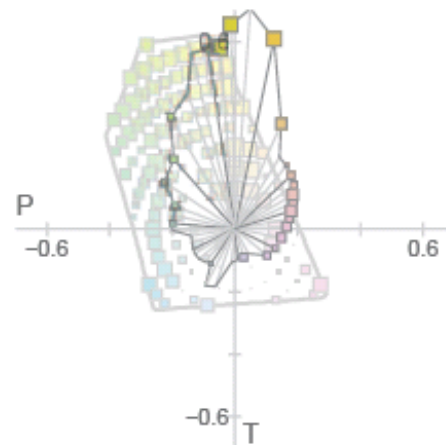
Munsell value = 6.0
IPT brightness = 0.6032



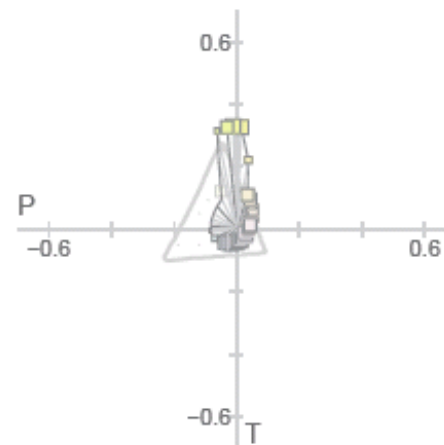
Munsell value = 7.0
IPT brightness = 0.7041



Munsell value = 8.0
IPT brightness = 0.8106

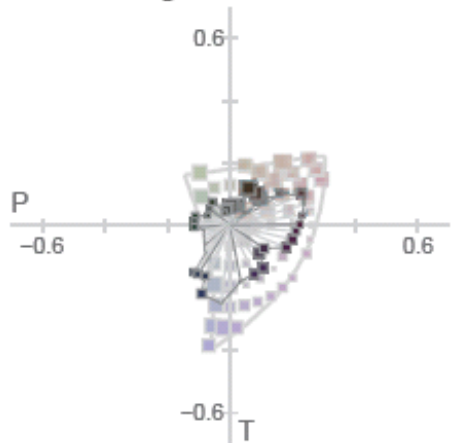


Munsell value = 9.0
IPT brightness = 0.9337

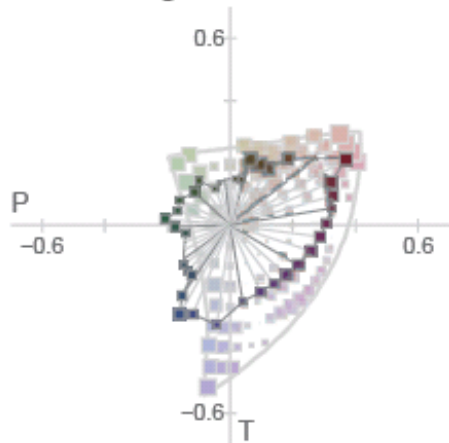


Comparison of Munsell/sRGB

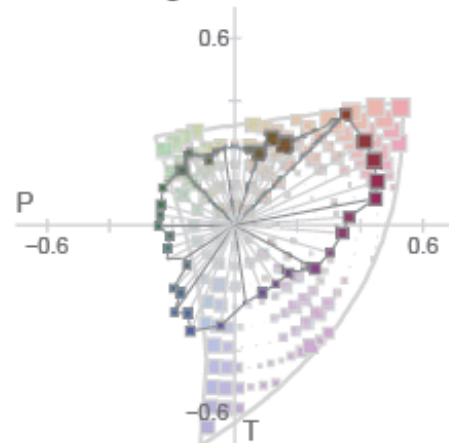
Munsell value = 2.0
IPT brightness = 0.2317



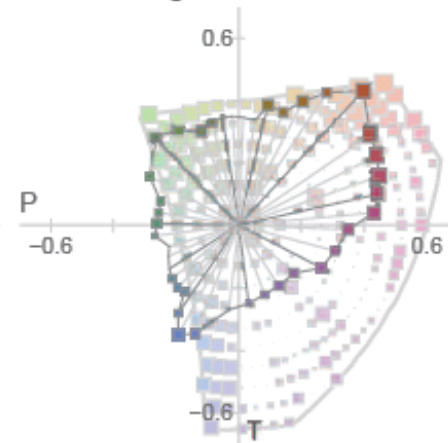
Munsell value = 3.0
IPT brightness = 0.3179



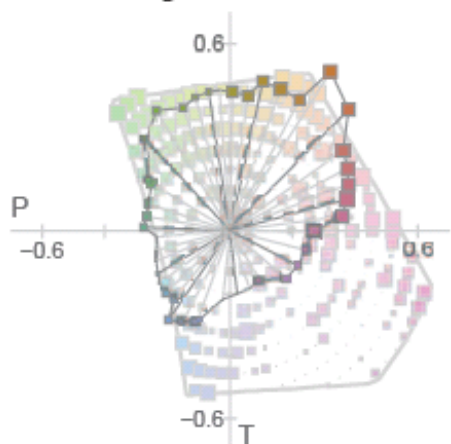
Munsell value = 4.0
IPT brightness = 0.4100



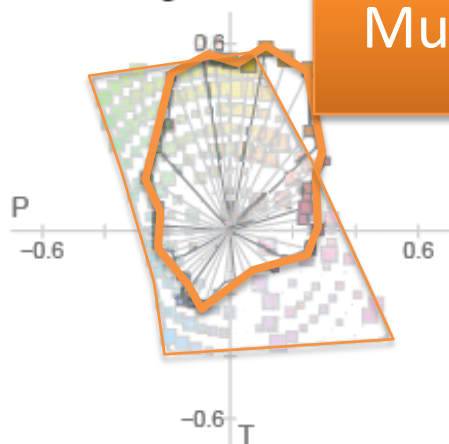
Munsell value = 5.0
IPT brightness = 0.5051



Munsell value = 6.0
IPT brightness = 0.6032

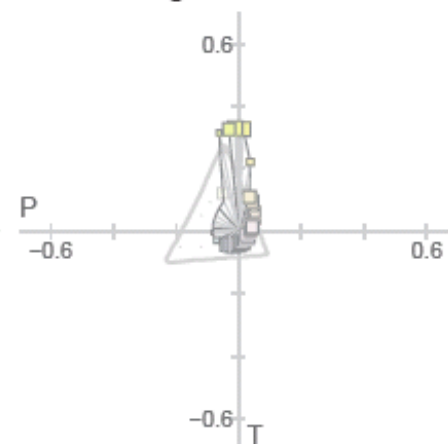


Munsell value = 7.0
IPT brightness = 0.7013



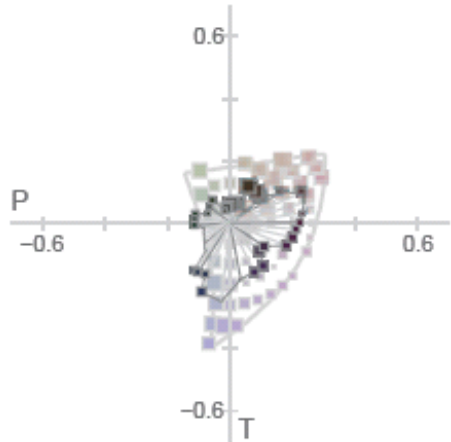
Munsell Surface

Munsell value = 9.0
IPT brightness = 0.9337

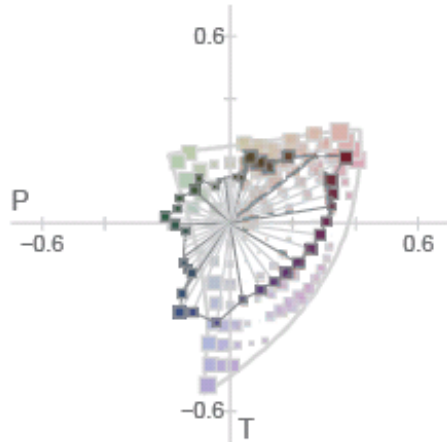


Comparison of Munsell/sRGB

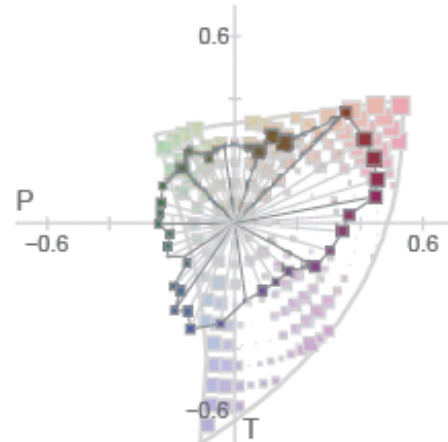
Munsell value = 2.0
IPT brightness = 0.2317



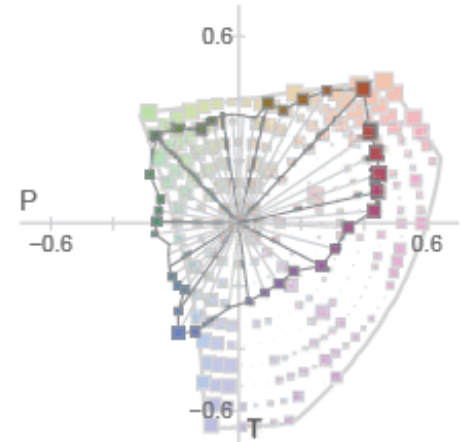
Munsell value = 3.0
IPT brightness = 0.3179



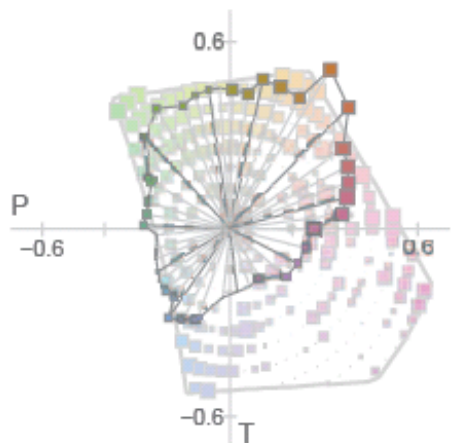
Munsell value = 4.0
IPT brightness = 0.4100



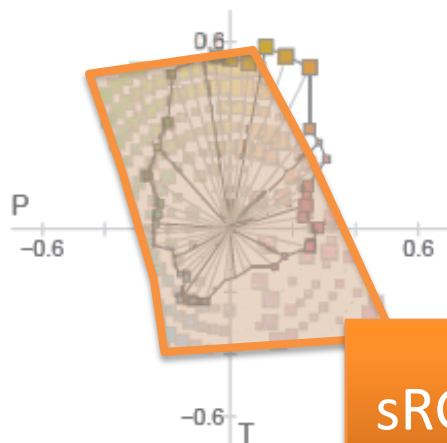
Munsell value = 5.0
IPT brightness = 0.5051



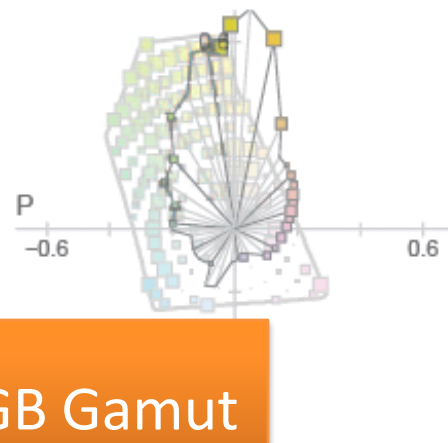
Munsell value = 6.0
IPT brightness = 0.6032



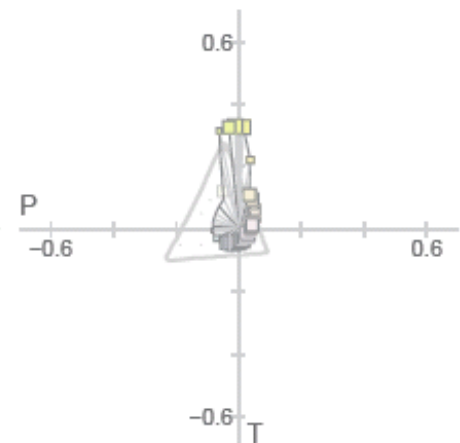
Munsell value = 7.0
IPT brightness = 0.7041



Munsell value = 8.0
IPT brightness = 0.8106



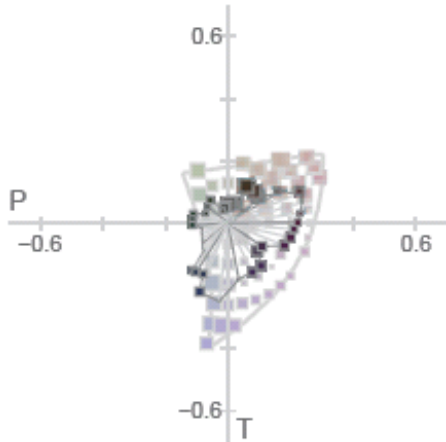
Munsell value = 9.0
IPT brightness = 0.9337



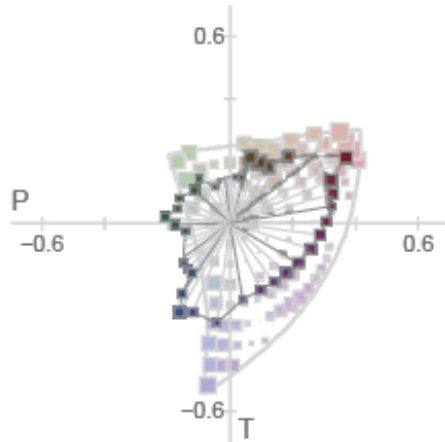
sRGB Gamut

Comparison of Munsell/sRGB

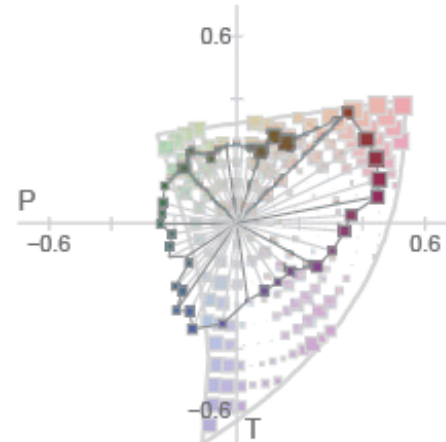
Munsell value = 2.0
IPT brightness = 0.2317



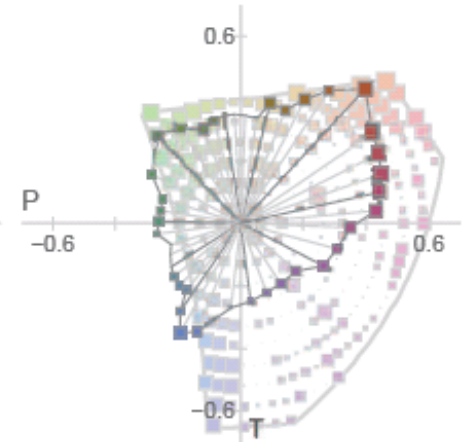
Munsell value = 3.0
IPT brightness = 0.3179



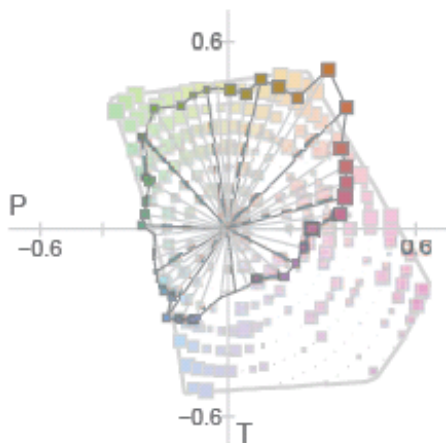
Munsell value = 4.0
IPT brightness = 0.4100



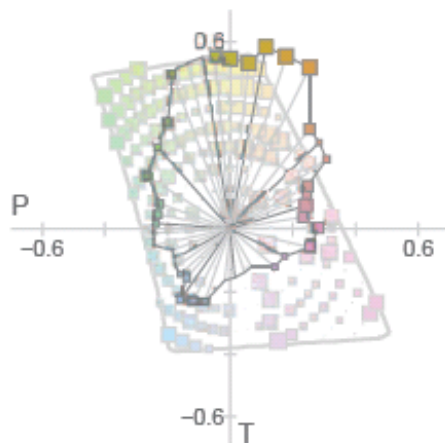
Munsell value = 5.0
IPT brightness = 0.5051



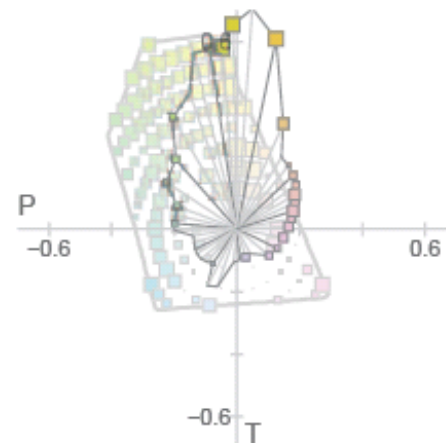
Munsell value = 6.0
IPT brightness = 0.6032



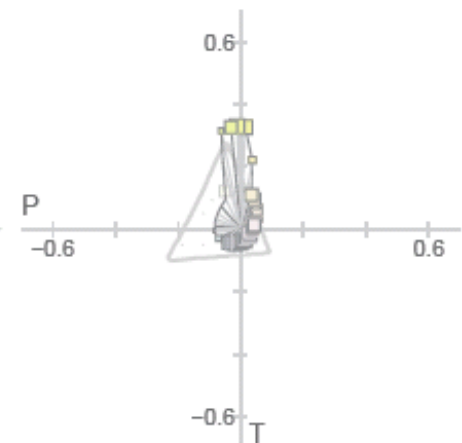
Munsell value = 7.0
IPT brightness = 0.7041



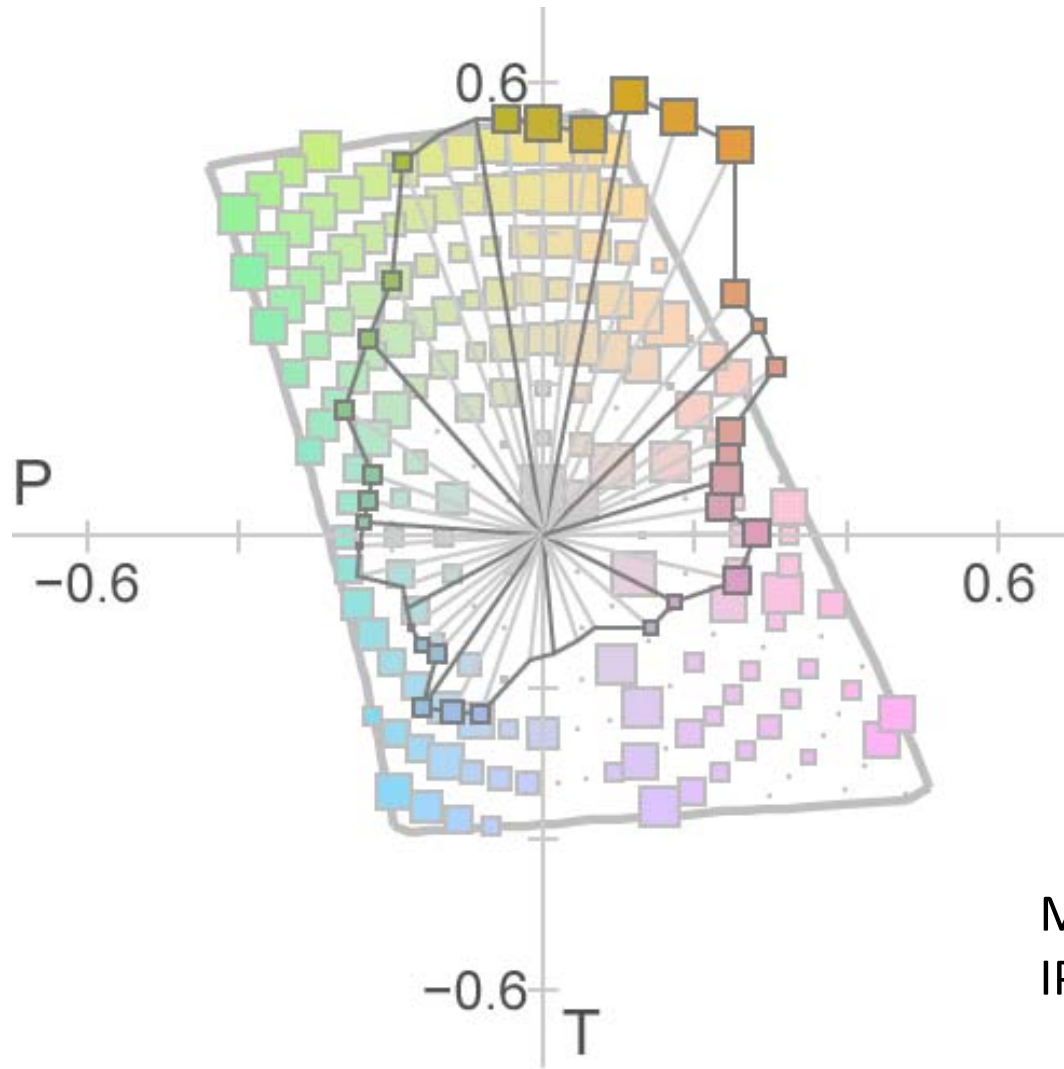
Munsell value = 8.0
IPT brightness = 0.8106



Munsell value = 9.0
IPT brightness = 0.9337

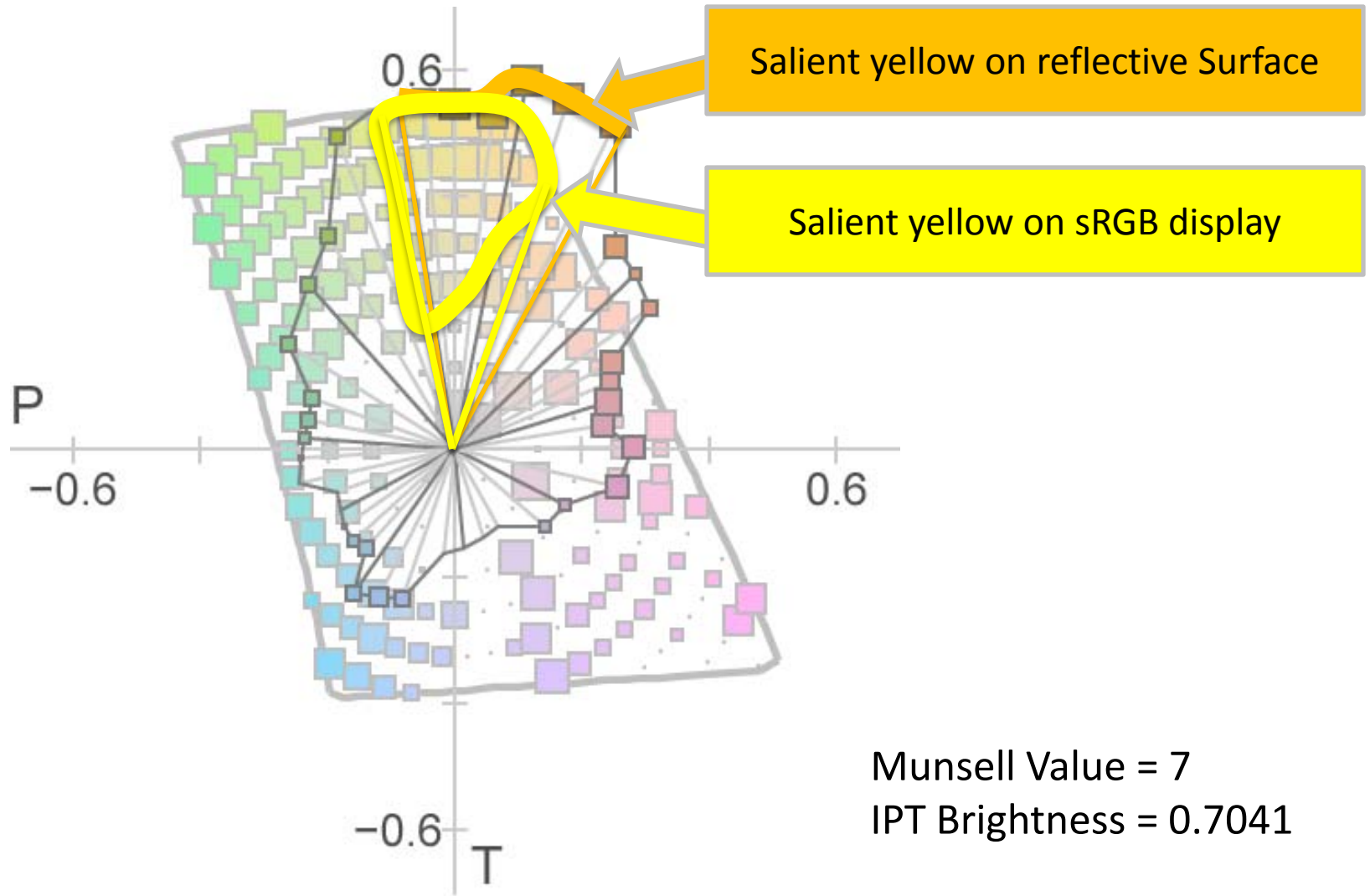


Comparison at Munsell Value=7



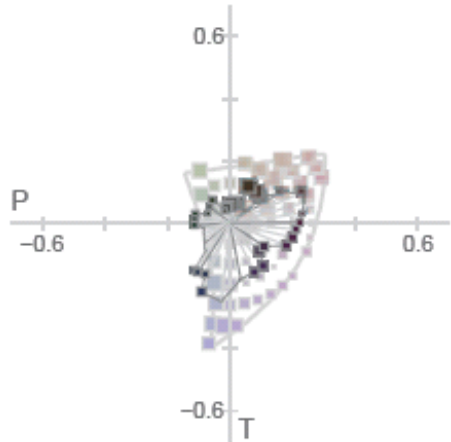
Munsell Value = 7
IPT Brightness = 0.7041

Comparison at Munsell Value=7

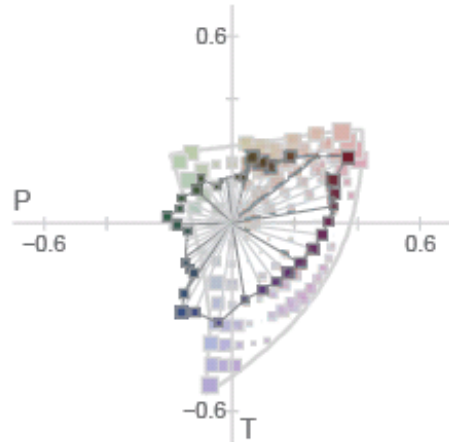


Saliency Differs for Munsell/sRGB

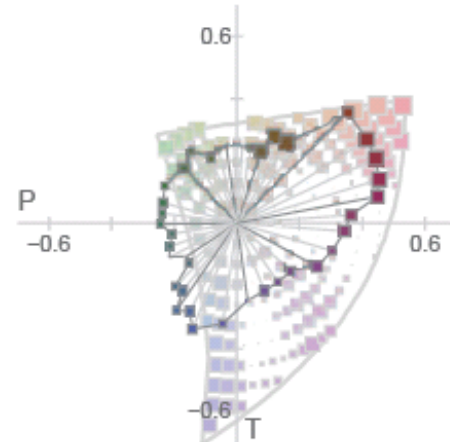
Munsell value = 2.0
IPT brightness = 0.2317



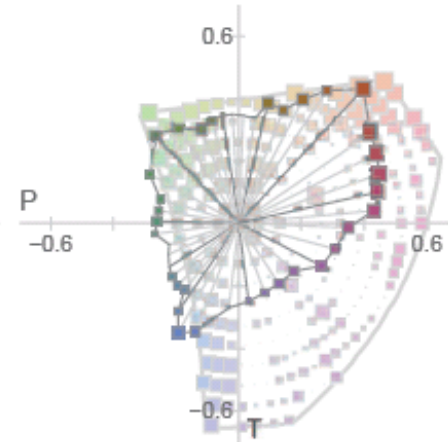
Munsell value = 3.0
IPT brightness = 0.3179



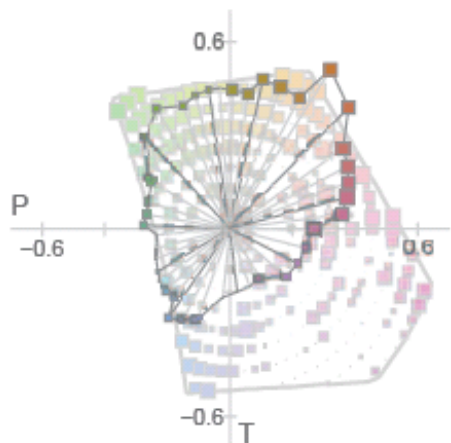
Munsell value = 4.0
IPT brightness = 0.4100



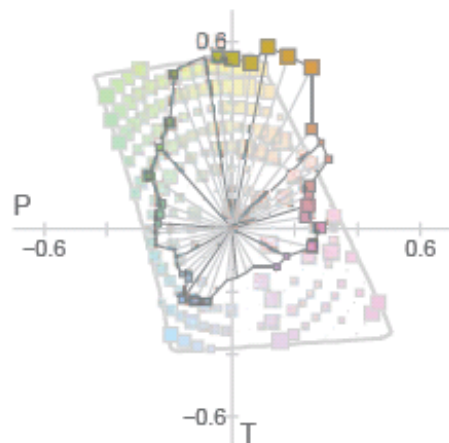
Munsell value = 5.0
IPT brightness = 0.5051



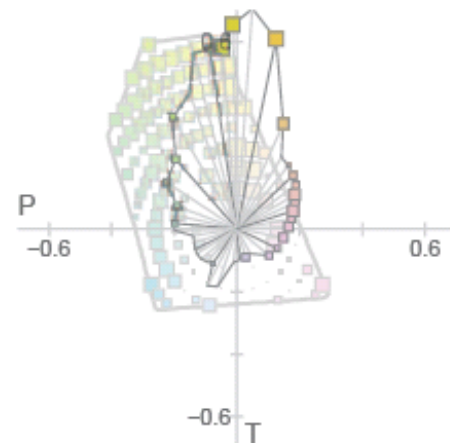
Munsell value = 6.0
IPT brightness = 0.6032



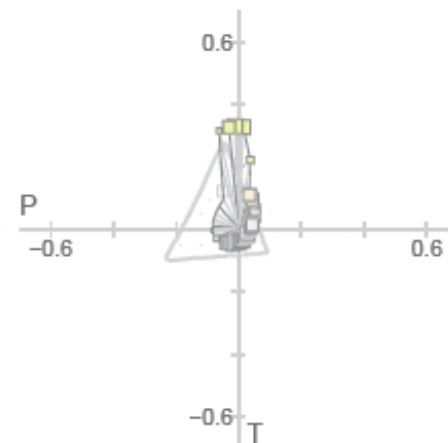
Munsell value = 7.0
IPT brightness = 0.7041



Munsell value = 8.0
IPT brightness = 0.8106



Munsell value = 9.0
IPT brightness = 0.9337



Overview

- Introduction
 - Color naming and categories
 - Previous work
 - Goals
- Categorical association
 - Probabilistic framework
 - Results
- **Summary**

Summary

- Categorical association between colors
 - Non-parametric model
 - Captured details and was robust on a large noisy dataset
 - Inclusion of all color words
 - Merged cross-linguistic data
 - Identified contributions from emerging non-basic terms
 - Computational tools
 - Saliency based on entropy
 - Saliency on Munsell surface and for sRGB Gamut